

# SM (SMX)

32 THREADS = 1 WARP

N WARPS = 1 BLOCK

& 32

---

$N = N + K$   
READ N  
ADD K  
WRITE N

RACE

INTERLEAVING

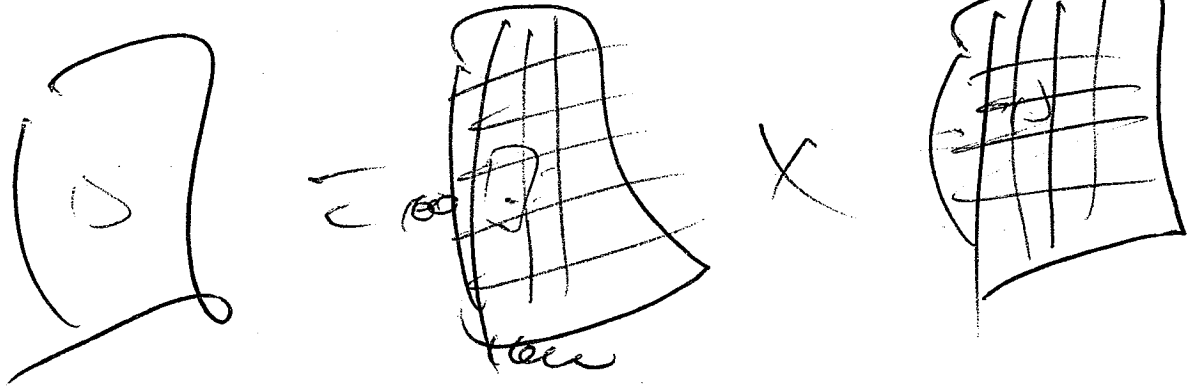
0 1 2 3

$T_0=0$   $T_1=0$   $T_2=0$   $T_3=0$

$T_0=1$   $T_1=1$   $T_2=1$

---

$S_0$   $S_1$   $S_2$   $S_3$   
 $T_0$   $T_1$   $T_2$   $T_3$



ADD 400M PAIRS = 30μsec

$$\frac{3 \times 10^2}{4 \times 10^9} = \frac{3}{4} \times 10^{-10} = \underline{\underline{.07 \mu\text{SEC}}}$$

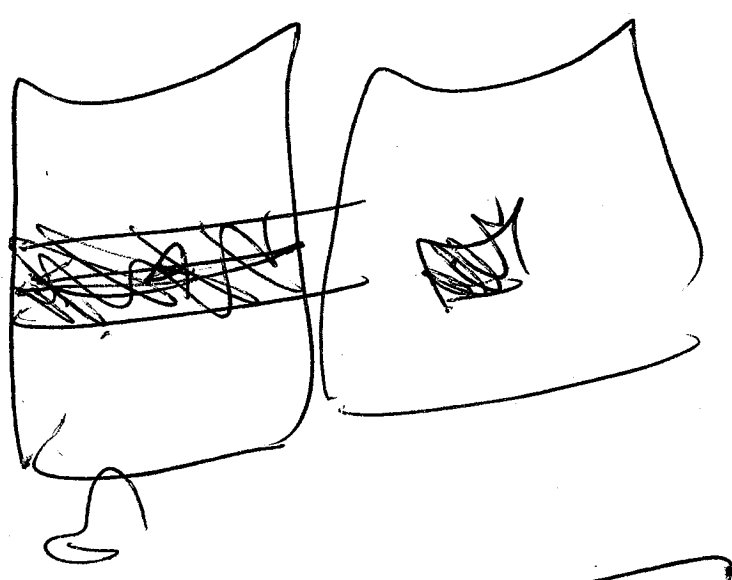
```
const int n = 1000;  
const int N2 = n * n;  
int a[n][n];
```

```
int *p = malloc(N2 * sizeof(int));  
if (p == 0) exit(1);
```

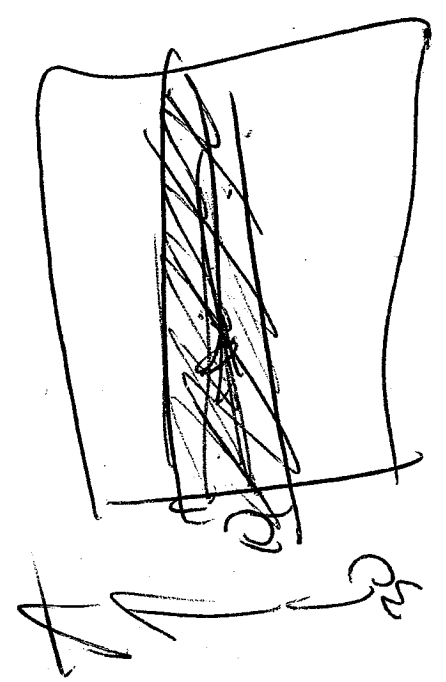
```
func  
int f2(int x, int y) {  
    return x + y; }  
}
```

```
int  
x + f2(x, y) =
```

2666



$$AD_{10} = \sum_K A_{11K} B_{1K}$$



FILE WIDTH = 10  
 WIDTH = 30

3/2/15

THREAD  $\frac{32}{}$  WARP

$\leq 1024$  BLOCK

SM: 48KB SHARE

---

RESOURCE LIMITS

# REGS

SHARED MEM.

# TRANSFORM

## VECTORS

$$W_a = U_a + V_c$$

### COPY

$$W_a = V_c$$

### COPY IF

SUPPOSE YOU WANT TO COPY  
EVEN # FROM

- 3 1 4 1 5 9 2 6 5
- 0 0 1 0 0 0 1 1 0
- 4 2 6

IN 0 1 2 3 4 5 6 7

STENCIL 0 1 1 0 0 1 0 1

OUT 1 2 5 7

3/12/15 - 2

(N 3 4 5 9 2 6 7)

TRANS

(3,3) (1,1) (4,4) (1,5) (5,6) (9,4) (2,2) (6,6) (5,5)

RETURNS

(1,3) (1,4) (5,9) (2,6)

(1,4)

(2,9)

(1,9)

MAX

auto f = [ ] ( ) { } ;

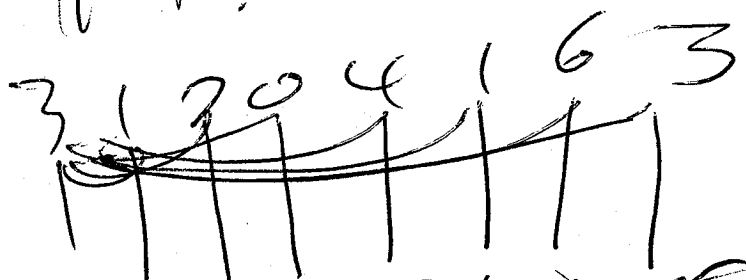
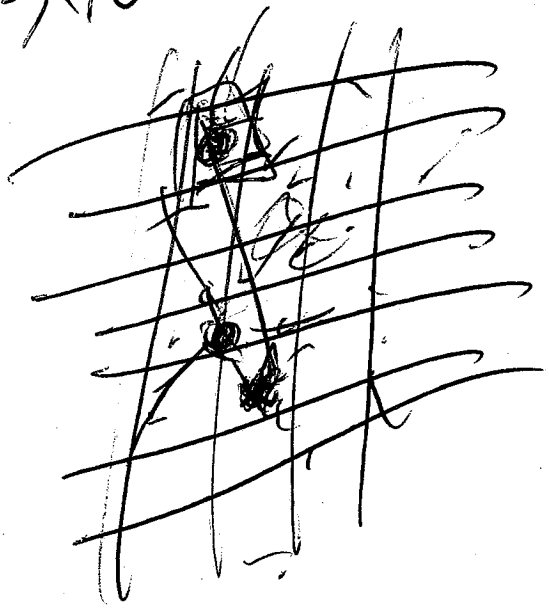
TREE

3/5/15

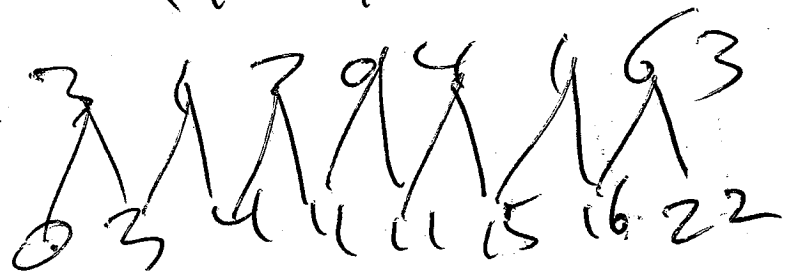


COMPACT

BIN APP → COSMOLOGY



0 3 4 11 11 15 16 22 ~~25~~





# RADIX SORT

2

TO SORT -

103, 123, 231, 001, 323,

BASE 4

232, 112, 201, 303, 220

FORM 4 OUTPUT Q, DIVIDE ON LAST DIGIT

0 220

1 231, 001, 201

2 232, 112

3 103, 123, 323, 303

REPEAT ON 2<sup>nd</sup> LAST DIGIT

0 001, 201, 103, 303

1 112

2 220, 123, 323

3 231, 232

REPEAT ON 1<sup>st</sup> DIGIT

0 001

1 103, 112, 123,

2 201, 220, 231, 232

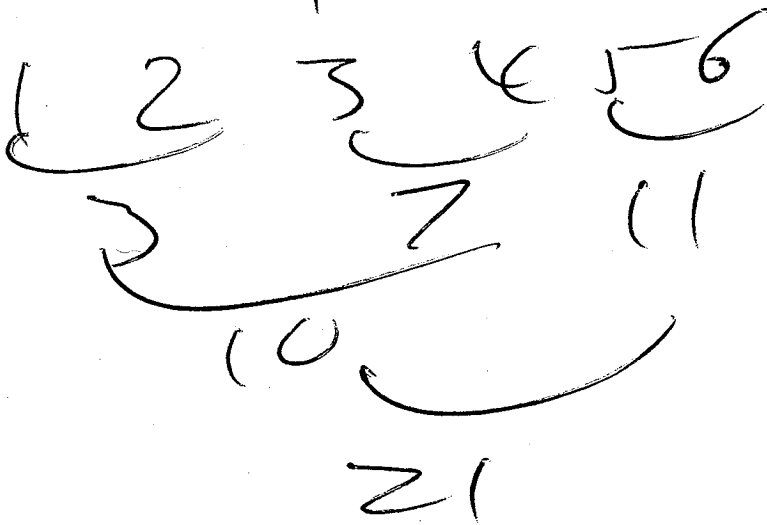
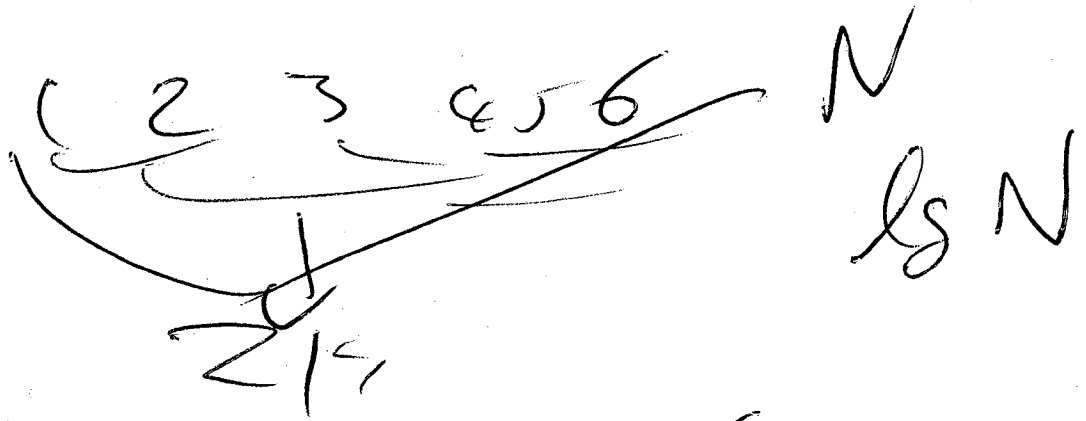
3 303, 323

ARRAY IS NOW SORTED

COST  
32  
17 MIN

REDUCE

3



SPLIT

3 1 4 1 5 9 2 6 5

3 1 4 1 5 2 5 | 9 6

QUICK SORT

⑤

# HISTOGRAM

K

IN: 3 1 4 1 5 9 2 6 5

OUT: 0 1 2 3 4 5 6 7 8 9  
0 2 1 1 1 2 1 0 0 1

1 2 3 4 5 6 7 8 9  
0 1 3 6 10 15 21 20 14

5E6M SCAN: BARRIER

1 2 3 4 5 6 7 8 9  
0 1 3 6 10 15 21 30  
1 2 3 4 5 6 7 8 9  
0 1 3 6 10 15 21 30

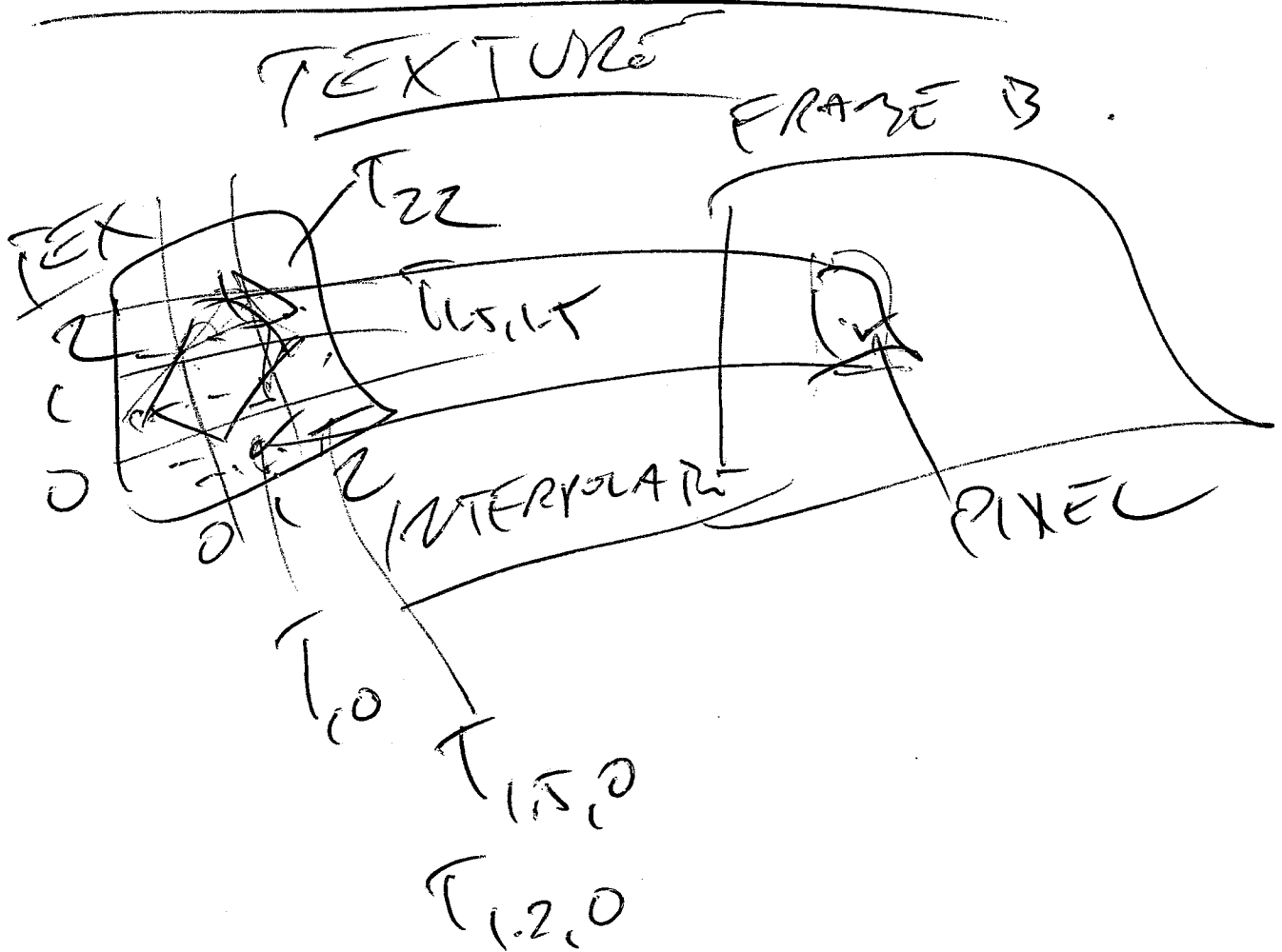
USE SORT TO HISTO

5

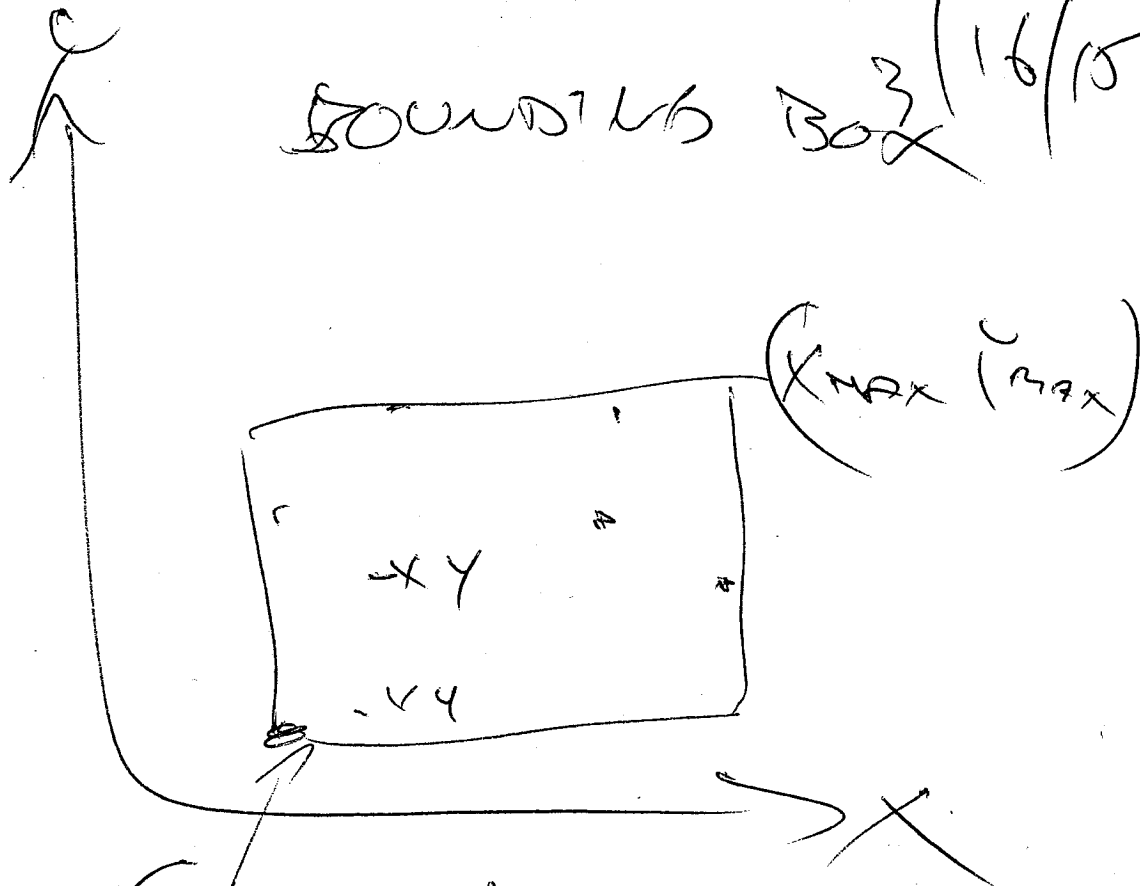
2 1 4 1 5 9 2 6 5

↓ SORT

1	1	2	3	4	5	5	6	9
2	1	1	1	2	2	1	0	1

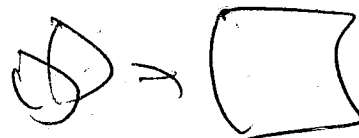
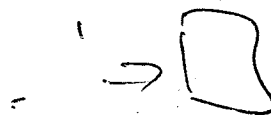
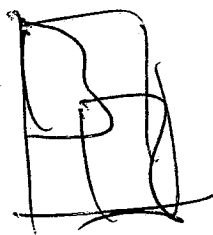


FOUNDING BOX 3/16/15

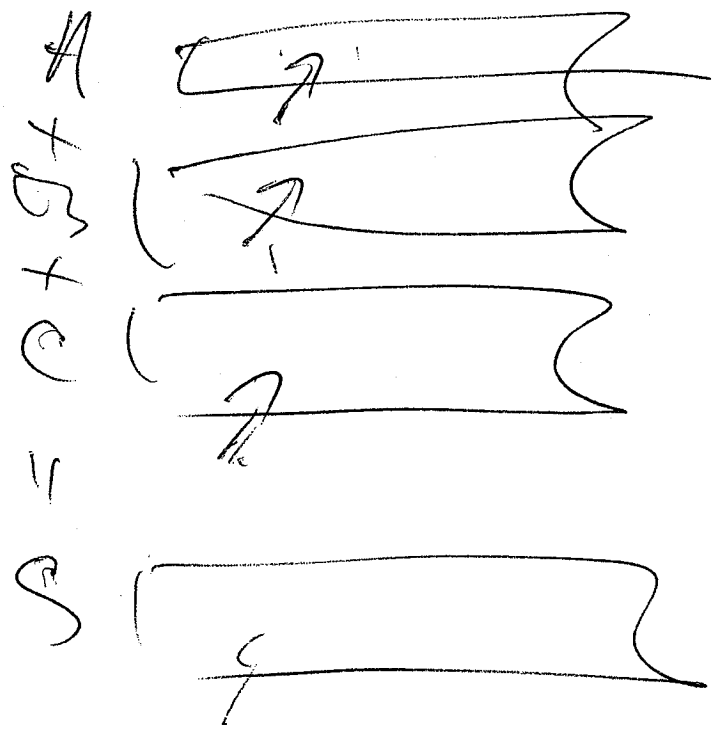


$(x_{min}, y_{min})$

REDUCTION



3/16/0



OLD STRUCT {INT A, B, C;}

VECTOR S(100)

ARRAY OF STRUCT SOA  
SLOW

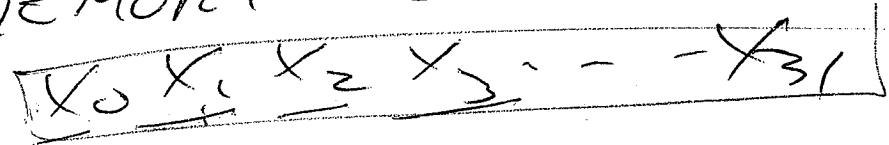
STRUCT OF ARRAY SOA FAST

ZIP ITERATOR

TUPLE PAIR, TRIPLE --- 9-11

get<sub>i</sub>(+)  
2

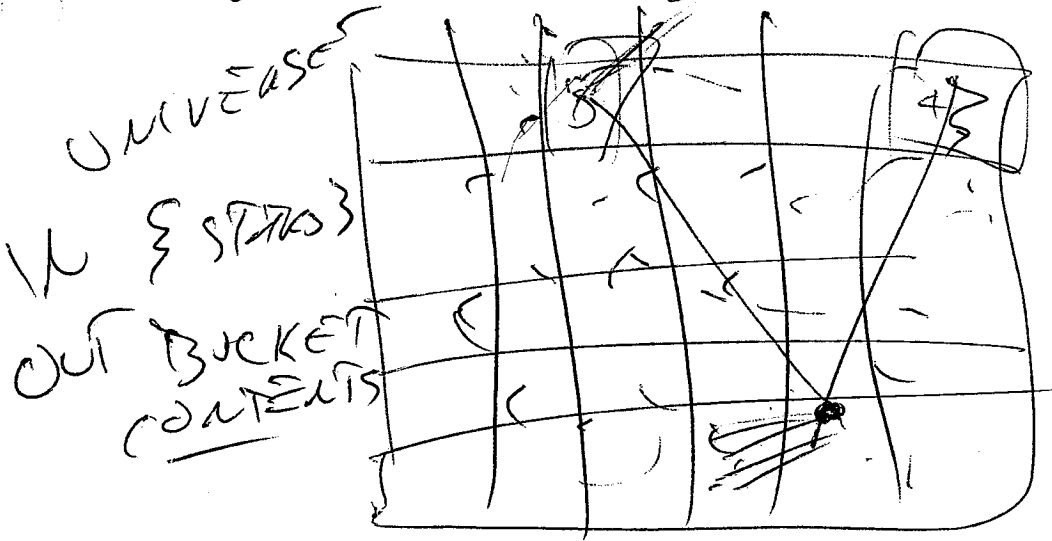
MEMORY COALESE



$x_0 x_1 x_2 x_3 \dots$

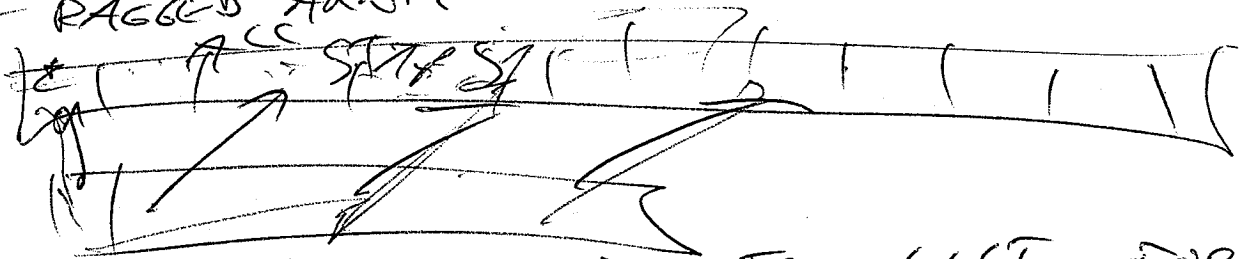
EXPAND APP.  
BUCKET SORT

3



~~BR~~ LINKED LIST  
VECTORS

GOOD RAGGED ARRAY



DOPE  
VECTOR

POINTS TO START OF STAR LIST FOR  
EACH CELL.

3/19/15 - 1

INNER PRODUCT

$$\sum a_i b_i$$

$$\begin{array}{r}
 a: \quad ( \quad 2 \quad 3 \\
 b: \quad ( \quad 4 \quad 5 \quad 6 \\
 * \\
 \quad \quad 4 \quad 10 \quad 18 \\
 + \\
 \quad \quad \quad 32
 \end{array}$$

CAN GENERALIZE \* +  
≠

$$\begin{array}{r}
 a \quad ( \quad 1 \quad 2 \quad 2 \quad 2 \quad 3 \quad 4 \quad 4 \\
 b \quad ( \quad 1 \quad 2 \quad 2 \quad 2 \quad 3 \quad 4 \quad 4 \\
 * \\
 \quad \quad 0 \quad 1 \quad 0 \quad 0 \quad 1 \quad 1 \quad 0 \\
 + \rightarrow 3
 \end{array}$$

4 UNIQUE KEYS

REDUCE (2 3 4) → 15

REDUCE BY KEY REDUCES BLOCKS.

KEY: (1, 2, 2, 3)

TO REDUCE:

$$\begin{array}{r}
 ( \quad 2 \quad 3 \quad 4 \quad 5 \\
 \underline{\quad 3 \quad 7 \quad 5}
 \end{array}$$

KEY: (2 3 4 5 6)

V.

$$\begin{array}{r}
 \underline{\quad 3 \quad 4 \quad 5 \quad 9} \\
 3 \quad 1 \quad 4 \quad 1 \quad 5 \quad 9
 \end{array}$$

$$\begin{array}{r}
 ( \quad 1 \quad 1 \quad 1 \quad 1 \quad 1 \\
 \underline{\quad 3 \quad 1 \quad 4 \quad 1 \quad 5 \quad 9} \\
 2 \quad 3
 \end{array}$$



SORTED VEC	<u>11</u>	<u>222</u>	3	<u>44</u>
→ KEYS				
TO REID	<u>11</u>	<u>111</u>	1	111
MULTIPLICITIES	2	3	1	2

SET OPS

A = 3 1 4 5 9  
 B = 2 7 1 8 3

$5 \leq |A \cup B| \leq 10$

EXPAND

V	0	10	20	30	40
C	2	1	0	3	1

OUT: ~~00~~ 10 30 30 30 40

REDUCE C TO GET OUT SIZE = 7

EX SCAN C : 0 2 3 3 6

SCATTER

V: 3 1 4 5 9  
 M: 2 7 8 3 0

O: 9 1 3 5 2 2 1 4 1

EXPAND

3

V	0	10	20	30	40
C	2	1	0	3	1

OUT	0	0	<u>10</u>	<u>30</u>	<u>30</u>	<u>30</u>	<u>40</u>
-----	---	---	-----------	-----------	-----------	-----------	-----------

EX SCAR	0	2	3	3	6
---------	---	---	---	---	---

SCATTER	0	1	2	3	4	<del>5</del>
---------	---	---	---	---	---	--------------

WITH	0	2	3	3	6
------	---	---	---	---	---

0	0	<del>4</del>	3	0	0	4
---	---	--------------	---	---	---	---

<u>0</u>	<u>0</u>	<u>1</u>	<u>3</u>	<u>3</u>	<u>3</u>	<del>4</del>
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GATHER	0	0	10	30	30	30	40
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100 →

3/29/15 - 1

↑ 600 ↓	314	134
	159	159
	265	256
	<u>395</u>	359

PAIRS (row #, elt contents)

(1,3), (1,1), (1,4), (2,1), (2,5), (2,9),  
 (3,2), (3,6), (3,5), (4,3), (4,9), (4,5)

sort on 2nd

(1,1), (2,1), (3,2), (1,3), (4,3), (1,4), (2,5),  
 (3,5), (4,5), (3,6), (2,9), (4,9)

STABLE SORT ON 1st

(1,1), (1,3), (1,4), (2,1), (2,5), (2,9), (3,2),  
 (3,5), (3,6), (4,3), (4,5), (4,9)

1: 1, 3, 4

3: 2, 5, 6

2: 1, 5, 9

4: 3, 5, 9

# How RADIX SORT WORKS

2

12, 23, 13, 31, 22, 33, 11

STABLE SORT ON UNITS

31, 11, 12, 22, 23, 13, 33

STABLE SORT ON TENS

11, 12, 13, 22, 23, 31, 33

---

REDUCE

IN 1 2 3 4 5

OUT: 15

REDUCE BY KEY

IN 1 2 3 4 5  
KEYS 1 1 2 3 3

OUT 3, 3, 9

---

IN 1 1 1 1 1 1 1  
KEYS A A B C C C D  
OUT 2, 1, 3, 1

# DENSE HISTO

3

DATA 3 1 4 1 5 9 2 | 6 5 3 5 9

SORT 1 1 2 3 3 4 5 5 5 6 9 9  
~~0 1 2 3 4 5 6 7 8 9 10 11~~

~~NEED 10 BINS~~

0 1 2 3 4 5 6 7 8 9 10 11

0 2 3 5 6 9 10 10 10 12

HISTO DIF

2 1 2 1 3 1 0 0 2 2 HISTO