

CUFFT LIBRARY USER'S GUIDE

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Chapter 1. INTRODUCTION

This document describes cuFFT, the NVIDIA® CUDATM Fast Fourier Transform (FFT) product. It consists of two separate libraries: cuFFT and cuFFTW. The cuFFT library is designed to provide high performance on NVIDIA GPUs. The cuFFTW library is provided as a porting tool to enable users of FFTW to start using NVIDIA GPUs with a minimum amount of effort.

The FFT is a divide-and-conquer algorithm for efficiently computing discrete Fourier transforms of complex or real-valued data sets. It is one of the most important and widely used numerical algorithms in computational physics and general signal processing. The cuFFT library provides a simple interface for computing FFTs on an NVIDIA GPU, which allows users to quickly leverage the floating-point power and parallelism of the GPU in a highly optimized and tested FFT library.

The cuFFT product supports a wide range of FFT inputs and options efficiently on NVIDIA GPUs. This version of the cuFFT library supports the following features:

- Algorithms highly optimized for input sizes that can be written in the form $2^a \times 3^b \times 5^c \times 7^d$. In general the smaller the prime factor, the better the performance, i.e., powers of two are fastest.
- ► An *O*(*n*log *n*) algorithm for every input data size
- Single-precision (32-bit floating point) and double-precision (64-bit floating point).
 Single-precision transforms have higher performance than double-precision transforms.
- ► Complex and real-valued input and output. Real valued input or output require less computations and data than complex values and often have faster time to solution. Types supported are:
 - C2C Complex input to complex output
 - ▶ R2C Real input to complex output
 - C2R Symmetric complex input to real output
- ▶ 1D, 2D and 3D transforms
- ► Execution of multiple 1D, 2D and 3D transforms simultaneously. These batched transforms have higher performance than single transforms.
- ► In-place and out-of-place transforms
- ► Arbitrary intra- and inter-dimension element strides (strided layout)

- FFTW compatible data layouts
- Execution of transforms across two or four GPUs
- ▶ Streamed execution, enabling asynchronous computation and data movement
- ► Transform sizes up to 512 million elements in single precision and up to half that in double precision in any dimension, limited by the type of transform chosen and the available GPU memory

The cuFFTW library provides the FFTW3 API to facilitate porting of existing FFTW applications.

Chapter 2. USING THE CUFFT API

This chapter provides a general overview of the cuFFT library API. For more complete information on specific functions, see cuFFT API Reference. Users are encouraged to read this chapter before continuing with more detailed descriptions.

The Discrete Fourier transform (DFT) maps a complex-valued vector x_k (*time domain*) into its *frequency domain representation* given by:

$$X_k = \sum_{n=0}^{N-1} x_n e^{-2\pi i \frac{kn}{N}}$$

where X_k is a complex-valued vector of the same size. This is known as a *forward* DFT. If the sign on the exponent of e is changed to be positive, the transform is an *inverse* transform. Depending on N, different algorithms are deployed for the best performance.

The cuFFT API is modeled after FFTW, which is one of the most popular and efficient CPU-based FFT libraries. cuFFT provides a simple configuration mechanism called a *plan* that uses internal building blocks to optimize the transform for the given configuration and the particular GPU hardware selected. Then, when the *execution* function is called, the actual transform takes place following the plan of execution. The advantage of this approach is that once the user creates a plan, the library retains whatever state is needed to execute the plan multiple times without recalculation of the configuration. This model works well for cuFFT because different kinds of FFTs require different thread configurations and GPU resources, and the plan interface provides a simple way of reusing configurations.

Computing a number **BATCH** of one-dimensional DFTs of size **NX** using cuFFT will typically look like this:

2.1. Accessing cuFFT

The cuFFT and cuFFTW libraries are available as shared libraries. They consist of compiled programs ready for users to incorporate into applications with the compiler and linker. cuFFT can be downloaded from http://developer.nvidia.com/cufft. By selecting **Download CUDA Production Release** users are all able to install the package containing the CUDA Toolkit, SDK code samples and development drivers. The CUDA Toolkit contains cuFFT and the samples include **simplecuFFT**.

The Linux release for simplecuFFT assumes that the root install directory is /usr/local/cuda and that the locations of the products are contained there as follows. Modify the Makefile as appropriate for your system.

Product	Location and name	Include file
nvcc compiler	/bin/nvcc	
cuffT library	{lib, lib64}/libcufft.so	inc/cufft.h
cuffT library with Xt functionality	{lib, lib64}/libcufft.so	inc/cufftXt.h
cufftw library	{lib, lib64}/libcufftw.so	inc/cufftw.h

The most common case is for developers to modify an existing CUDA routine (for example, filename.cu) to call cuFFT routines. In this case the include file cufft.h or cufftXt.h should be inserted into filename.cu file and the library included in the link line. A single compile and link line might appear as

/usr/local/cuda/bin/nvcc [options] filename.cu ... -I/usr/local/ cuda/inc -L/usr/local/cuda/lib -lcufft

Of course there will typically be many compile lines and the compiler **g++** may be used for linking so long as the library path is set correctly.

Users of the FFTW interface (see FFTW Interface to cuFFT) should include cufftw.h and link with both cuFFT and cuFFTW libraries.

For the best performance input data should reside in device memory. Therefore programs in the cuFFT library assume that the data is in GPU memory. For example, if one of the execution functions is called with data in host memory, the program will return <code>CUFFT_EXEC_FAILED</code>. Programs in the cuFFTW library assume that the input data is in host memory since this library is a porting tool for users of FFTW. If the data resides in GPU memory, the program will abort.

2.2. Fourier Transform Setup

The first step in using the cuFFT Library is to create a plan using one of the following:

- cufftPlan1D() / cufftPlan2D() / cufftPlan3D() Create a simple plan for a 1D/2D/3D transform respectively.
- cufftPlanMany() Creates a plan supporting batched input and strided data layouts.

Among the plan creation functions, cufftPlanMany() allows use of more complicated data layouts and batched executions. Execution of a transform of a particular size and type may take several stages of processing. When a plan for the transform is generated, cuFFT derives the internal steps that need to be taken. These steps may include multiple kernel launches, memory copies, and so on. In addition, all the intermediate buffer allocations (on CPU/GPU memory) take place during planning. These buffers are released when the plan is destroyed. In the worst case, the cuFFT Library allocates space for 8*batch*n[0]*..*n[rank-1] cufftComplex or cufftDoubleComplex elements (where batch denotes the number of transforms that will be executed in parallel, rank is the number of dimensions of the input data (see Multidimensional Transforms) and n[] is the array of transform dimensions) for single and doubleprecision transforms respectively. Depending on the configuration of the plan, less memory may be used. In some specific cases, the temporary space allocations can be as low as 1*batch*n[0]*..*n[rank-1] cufftComplex or cufftDoubleComplex elements. This temporary space is allocated separately for each individual plan when it is created (i.e., temporary space is not shared between the plans).

The next step in using the library is to call an execution function such as **cufftExecC2C()** (see Parameter cufftType) which will perform the transform with the specifications defined at planning.

One can create a cuFFT plan and perform multiple transforms on different data sets by providing different input and output pointers. Once the plan is no longer needed, the <code>cufftDestroy()</code> function should be called to release the resources allocated for the plan.

2.3. Fourier Transform Types

Apart from the general complex-to-complex (C2C) transform, cuFFT implements efficiently two other types: real-to-complex (R2C) and complex-to-real (C2R). In many

practical applications the input vector is real-valued. It can be easily shown that in this case the output satisfies Hermitian symmetry ($X_k = X_{N-k'}^*$ where the star denotes complex conjugation). The converse is also true: for complex-Hermitian input the inverse transform will be purely real-valued. cuFFT takes advantage of this redundancy and works only on the first half of the Hermitian vector.

Transform execution functions for single and double-precision are defined separately as:

- cufftExecC2C() / cufftExecZ2Z() complex-to-complex transforms for single/ double precision.
- **cufftExecR2C()** / **cufftExecD2Z()** real-to-complex forward transform for single/double precision.
- cufftExecC2R() / cufftExecZ2D() complex-to-real inverse transform for single/double precision.

Each of those functions demands different input data layout (see Data Layout for details).

2.4. Data Layout

In the cuFFT Library, data layout depends strictly on the configuration and the transform type. In the case of general complex-to-complex transform both the input and output data shall be a **cufftComplex/cufftDoubleComplex** array in single- and double-precision modes respectively. In C2R mode an input array $(x_1, x_2, ..., x_{ \square \frac{N}{2} \square + 1})$ of only non-redundant complex elements is required. The output array $(X_1, X_2, ..., X_N)$ consists of **cufftReal/cufftDouble** elements in this mode. Finally, R2C demands an input array $(X_1, X_2, ..., X_N)$ of real values and returns an array $(x_1, x_2, ..., x_{ \square \frac{N}{2} \square + 1})$ of non-redundant complex elements.

In real-to-complex and complex-to-real transforms the size of input data and the size of output data differ. For out-of-place transforms a separate array of appropriate size is created. For in-place transforms the user can specify one of two supported data layouts: **padded** or**native**(deprecated). The default is **padded** for FFTW compatibility.

In the **padded** layout output signals begin at the same memory addresses as the input data. Therefore input data for real-to-complex and output data for complex-to-real must be padded. In the **native**(deprecated) layout no padding is required and both input and output data are formed as arrays of adequate types and sizes.

Expected sizes of input/output data for 1-d transforms are summarized in the table below:

FFT type	input data size	output data size
C2C	X cufftComplex	X cufftComplex
C2R	$\left[\left[\frac{X}{2}\right]\right] + 1$ cufftComplex	X cufftReal
R2C*	X cufftReal	$\left[\frac{x}{2} \right] + 1$ cufftComplex

The real-to-complex transform is implicitly a forward transform. For an in-place real-to-complex transform where FFTW compatible output is desired, the input size must be padded to $\left(\Box \frac{N}{2} \Box + 1 \right)$ complex elements. For out-of-place transforms, input and output sizes match the logical transform size N and the non-redundant size $\Box \frac{N}{2} \Box + 1$, respectively.

The complex-to-real transform is implicitly inverse. For in-place complex-to-real FFTs where FFTW compatible output is selected (default padding mode), the input size is assumed to be $\frac{N}{2}\Box+1$ cufftComplex elements. Note that in-place complex-to-real FFTs may overwrite arbitrary imaginary input point values when non-unit input and output strides are chosen. For out-of-place transforms, input and output sizes match the logical transform non-redundant size $\Box \frac{N}{2}\Box+1$ and size N, respectively.

2.4.1. FFTW Compatibility Mode

For some transform sizes, FFTW requires additional padding bytes between rows and planes of real-to-complex (R2C) and complex-to-real (C2R) transforms of rank greater than 1. (For details, please refer to the FFTW online documentation.)

One can disable FFTW-compatible layout using cufftSetCompatibilityMode() (deprecated). Setting the input parameter to
CUFFT_COMPATIBILITY_NATIVE disables padding and ensures compact data layout for the input/output data for Real-to-Complex/Complex-To-Real transforms.

The FFTW compatibility modes are as follows:

CUFFT_COMPATIBILITY_NATIVE mode disables FFTW compatibility and packs data most compactly.(this mode has been deprecated)

CUFFT_COMPATIBILITY_FFTW_PADDING supports FFTW data padding by inserting extra padding between packed in-place transforms for batched transforms (default).

CUFFT_COMPATIBILITY_FFTW_ASYMMETRIC guarantees FFTW-compatible output for non-symmetric complex inputs for transforms with power-of-2 size. This is only useful for artificial (that is, random) data sets as actual data will always be symmetric if it has come from the real plane. Enabling this mode can significantly impact performance.

CUFFT_COMPATIBILITY_FFTW_ALL enables full FFTW compatibility (both CUFFT_COMPATIBILITY_FFTW_PADDING and CUFFT_COMPATIBILITY_FFTW_ASYMMETRIC).

Refer to the FFTW online documentation for detailed FFTW data layout specifications.

The default mode is **CUFFT_COMPATIBILITY_FFTW_PADDING**

2.5. Multidimensional Transforms

Multidimensional DFT map a *d*-dimensional array x_n , where $\mathbf{n} = (n_1, n_2, ..., n_d)$ into its frequency domain array given by:

$$X_{\mathbf{k}} = \sum_{n=0}^{N-1} x_{\mathbf{n}} e^{-2\pi i \frac{\mathbf{k} \mathbf{n}}{\mathbf{N}}}$$

where $\frac{\mathbf{n}}{\mathbf{N}} = (\frac{n_1}{N_1}, \frac{n_2}{N_2}, \dots, \frac{n_d}{N_d})$, and the summation denotes the set of nested summations

$$\sum_{n_1=0}^{N_1-1N_2-1} \sum_{n_2=0}^{N_d-1} \dots \sum_{n_d=0}^{N_d-1}$$

cuFFT supports one-dimensional, two-dimensional and three-dimensional transforms, which can all be called by the same **cufftExec*** functions (see Fourier Transform Types).

Similar to the one-dimensional case, the frequency domain representation of real-valued input data satisfies Hermitian symmetry, defined as: $x_{(n_1,n_2,..,n_d)} = x_{(N_1-n_1,N_2-n_2,..,N_d-n_d)}^*$.

C2R and R2C algorithms take advantage of this fact by operating only on half of the elements of signal array, namely on: x_n for

$$\mathbf{n} \in \{1, ..., N_1\} \times ... \times \{1, ..., N_{d-1}\} \times \{1, ..., \Box \frac{N_d}{2} \Box + 1\}.$$

The general rules of data alignment described in Data Layout apply to higher-dimensional transforms. The following table summarizes input and output data sizes for multidimensional DFTs:

Dims	FFT type	Input data size	Output data size
	C2C	N_1 cufftComplex	N_1 cufftComplex
1D	C2R	$ \frac{N_1}{2} \Box + 1 $ cufftComplex	N_1 cufftReal
	R2C	N_1 cufftReal	$\lceil \frac{N_1}{2} \rceil + 1$ cufftComplex
	C2C	$\mathbf{N}_1\mathbf{N}_2$ cufftComplex	$\mathbf{N}_1\mathbf{N}_2$ cufftComplex
2D	C2R	$N_1 = \frac{N_2}{2} + 1$ cufftComplex	$N_1 N_2$ cufftReal
	R2C	$N_1 N_2$ cufftReal	$N_1 = \frac{N_2}{2} + 1$ cufftComplex
	C2C	$N_1N_2N_3$ cufftComplex	$N_1N_2N_3$ cufftComplex
3D	C2R	N_1N_2 $\Box \frac{N_3}{2}\Box +1$) cufftComplex	$N_1 N_2 N_3$ cufftReal
	R2C	$N_1 N_2 N_3$ cufftReal	N_1N_2 $\!$

For example, static declaration of a three-dimensional array for the output of an out-ofplace real-to-complex transform will look like this:

cufftComplex odata[N1][N2][N3/2+1];

2.6. Advanced Data Layout

The advanced data layout feature allows transforming only a subset of an input array, or outputting to only a portion of a larger data structure. It can be set by calling function:

```
cufftResult cufftPlanMany(cufftHandle *plan, int rank, int *n, int *inembed,
   int istride, int idist, int *onembed, int ostride,
   int odist, cufftType type, int batch);
```

Passing inembed or onembed set to NULL is a special case and is equivalent to passing n for each. This is same as the basic data layout and other advanced parameters such as istride are ignored.

If the advanced parameters are to be used, then all of the advanced interface parameters must be specified correctly. Advanced parameters are defined in units of the relevant data type (cufftReal, cufftDoubleReal, cufftComplex, or cufftDoubleComplex).

Advanced layout can be perceived as an additional layer of abstraction above the access to input/output data arrays. An element of coordinates [z][y][x] in signal number b in the batch will be associated with the following addresses in the memory:

```
input[ b*idist+x*istride]
output[ b*odist+x*ostride]

2D
input[b*idist+(x*inembed[1]+y)*istride]
output[b*odist+(x*onembed[1]+y)*ostride]

3D
input[b*idist+((x*inembed[1]+y)*inembed[2]+z)*istride]
output[b*odist+((x*inembed[1]+y)*onembed[2]+z)*ostride]
```

The istride and ostride parameters denote the distance between two successive input and output elements in the least significant (that is, the innermost) dimension respectively. In a single 1D transform, if every input element is to be used in the transform, istride should be set to 1; if every other input element is to be used in the transform, then istride should be set to 2. Similarly, in a single 1D transform, if it is desired to output final elements one after another compactly, ostride should be set to 1; if spacing is desired between the least significant dimension output data, ostride should be set to the distance between the elements.

The inembed and onembed parameters define the number of elements in each dimension in the input array and the output array respectively. The inembed[rank-1] contains the number of elements in the least significant (innermost) dimension of the input data excluding the istride elements; the number of total elements in the least significant dimension of the input array is then istride*inembed[rank-1]. The inembed[0] or onembed[0] corresponds to the most significant (that is, the outermost) dimension and is effectively ignored since the idist or odist parameter provides this information instead. Note that the size of each dimension of the transform should be less

than or equal to the **inembed** and **onembed** values for the corresponding dimension, that is $n[i] \le inembed[i]$, $n[i] \le onembed[i]$, where $i \in \{0, ..., rank - 1\}$.

The idist and odist parameters indicate the distance between the first element of two consecutive batches in the input and output data.

Internally cuFFT uses 32 bit unsigned integers to compute offsets. This results in a limitation on maximum transform size. The size of input data, including strides and batches, may not exceed 2^{32} bytes. This limitation also applies to output data and work area sizes.

2.7. Streamed cuFFT Transforms

Every cuFFT plan may be associated with a CUDA stream. Once so associated, all launches of the internal stages of that plan take place through the specified stream. Streaming of cuFFT execution allows for potential overlap between transforms and memory copies. (See the NVIDIA CUDA Programming Guide for more information on streams.) If no stream is associated with a plan, launches take place in stream(0), the default CUDA stream. Note that many plan executions require multiple kernel launches.

cufftSetStream() returns an error in the multiple GPU case as multiple GPU plans perform operations in their own streams.

2.8. Multiple GPU cuFFT Transforms

cuFFT supports using two or four GPUs connected to a CPU to perform Fourier Transforms whose calculations are distributed across the GPUs. An API has been defined to allow users to write new code or modify existing code to use this functionality.

Some existing functions such as the creation of a plan using **cufftCreate()** also apply in the multiple GPU case. Multiple GPU unique routines contain **xt** in their name.

The memory on the GPUs is managed by helper functions **cufftXtMalloc()** / **cufftXtFree()** and **cufftXtMemcpy()** using the **cudaLibXtDesc** descriptor.

Performance is a function of the bandwidth between the GPUs, the computational ability of the individual GPUs, and the type and number of FFT to be performed. The fastest performance is obtained using PCI Express 3.0 between the GPUs and ensuring that both GPUs are on the same switch. Note that multiple GPU execution is not guaranteed to solve a given size problem in a shorter time than single GPU execution.

The multiple GPU extensions to cuFFT are built on the extensible cuFFT API. The general steps in defining and executing a transform with this API are:

- cufftCreate() create an empty plan, as in the single GPU case
- cufftXtSetGPUs () define which GPUs are to be used
- Optional: cufftEstimate{1d,2d,3d,Many}() estimate the sizes of the work areas required. These are the same functions used in the single GPU case although the definition of the argument workSize reflects the number of GPUs used.

- cufftMakePlan{1d,2d,3d,Many} () create the plan. These are the same functions used in the single GPU case although the definition of the argument workSize reflects the number of GPUs used.
- Optional: cufftGetSize{1d,2d,3d,Many} () refined estimate of the sizes of the work areas required. These are the same functions used in the single GPU case although the definition of the argument workSize reflects the number of GPUs used.
- ▶ Optional: cufftGetSize() check workspace size. This is the same function used in the single GPU case although the definition of the argument workSize reflects the number of GPUs used.
- ▶ Optional: cufftXtSetWorkArea() do your own workspace allocation.
- cufftxtMalloc() allocate descriptor and data on the GPUs
- cufftXtMemcpy() copy data to the GPUs
- cufftXtExecDescriptorC2C()/cufftXtExecDescriptorZ2Z() execute the
 plan
- cufftXtMemcpy() copy data from the GPUs
- cufftXtFree() free any memory allocated with cufftXtMalloc()
- cufftDestroy() free cuFFT plan resources

2.8.1. Plan Specification and Work Areas

In the single GPU case a plan is created by a call to **cufftCreate()** followed by a call to **cufftMakePlan*()**. For multiple GPUs, the GPUs to use for execution are identified by a call to **cufftXtSetGPUs()** and this must occur after the call to **cufftCreate()** and prior to the call to **cufftMakePlan*()**.

Note that when <code>cufftMakePlan*()</code> is called for a single GPU, the work area is on that GPU. In a multiple GPU plan, the returned work area has multiple entries; one value per GPU. That is <code>workSize</code> points to a <code>size_t</code> array, one entry per GPU. Also the strides and batches apply to the entire plan across all GPUs associated with the plan.

Once a plan is locked by a call to **cufftMakePlan*()**, different descriptors may be specified in calls to **cufftXtExecDescriptor*()** to execute the plan on different data sets, but the new descriptors must use the same GPUs in the same order.

As in the single GPU case, cufftEstimateSize(Many,1d,2d,3d) () and cufftGetSize(Many,1d,2d,3d) () give estimates of the work area sizes required for a multiple GPU plan and in this case workSize points to a size_t array, one entry per GPU.

Similarly the actual work size returned by **cufftGetSize()** is a **size_t** array, one entry per GPU in the multiple GPU case.

2.8.2. Helper Functions

Multiple GPU cuFFT execution functions assume a certain data layout in terms of what input data has been copied to which GPUs prior to execution, and what output data resides in which GPUs post execution. cuFFT provides functions to assist users in manipulating data on multiple GPUs. These must be called after the call to cufftMakePlan*().

On a single GPU users may call **cudaMalloc()** and **cudaFree()** to allocate and free GPU memory. To provide similar functionality in the multiple GPU case, cuFFT includes **cufftXtMalloc()** and **cufftXtFree()** functions. The function **cufftXtMalloc()** returns a descriptor which specifies the location of these memories.

On a single GPU users may call **cudaMemcpy()** to transfer data between host and GPU memory. To provide similar functionality in the multiple GPU case, cuFFT includes **cufftXtMemcpy()** which allows users to copy between host and multiple GPU memories or even between the GPU memories.

All single GPU cuFFT FFTs return output the data in natural order, that is the ordering of the result is the same as if a DFT had been performed on the data. Some Fast Fourier Transforms produce intermediate results where the data is left in a permutation of the natural output. When batch is one, data is left in the GPU memory in a permutation of the natural output.

When **cufftXtMemcpy()** is used to copy data from GPU memory back to host memory, the results are in natural order regardless of whether the data on the GPUs is in natural order or permuted. Using **cufft_copy_device_to_device** allows users to copy data from the permuted data format produced after a single transform to the natural order on GPUs.

2.8.3. Multiple GPU 2D and 3D Transforms on Permuted Input

For single 2D or 3D transforms on multiple GPUs, when **cufftXtMemcpy()** distributes the data to the GPUs, the array is divided on the X axis. E.G. for two GPUs half of the X dimenson points, for all Y (and Z) values, are copied to each of the GPUs. When the transform is computed, the data are permuted such that they are divided on the Y axis. I.E. half of the Y dimension points, for all X (and Z) values are on each of the GPUs.

When cuFFT creates a 2D or 3D plan for a single transform on multiple GPUs, it actually creates two plans. One plan expects input to be divided on the X axis. The other plan expects data to be divided on the Y axis. This is done because many algorithms compute a forward FFT, then perform some point-wise operation on the result, and then compute the inverse FFT. A memory copy to restore the data to the original order would be expensive. To avoid this, **cufftxtMemcpy** and **cufftxtExecDescriptor()** keep track of the data ordering so that the correct operation is used.

The ability of cuFFT to process data in either order makes the following sequence possible.

- cufftCreate() create an empty plan, as in the single GPU case
- cufftXtSetGPUs () define which GPUs are to be used
- cufftMakePlan{1d,2d,3d,Many}() create the plan.
- cufftXtMalloc() allocate descriptor and data on the GPUs
- cufftXtMemcpy () copy data to the GPUs
- cufftXtExecDescriptorC2C()/cufftXtExecDescriptorZ2Z() compute the forward FFT
- ▶ userFunction() modify the data in the frequency domain

- cufftXtExecDescriptorC2C()/cufftXtExecDescriptorZ2Z() compute the inverse FFT
- Note that it was not necessary to copy/permute the data between execute calls
- cufftXtMemcpy () copy data to the host
- cufftXtFree() free any memory allocated with cufftXtMalloc()
- cufftDestroy() free cuFFT plan resources

2.8.4. Supported Functionality

In version 7.0 only a subset of single GPU functionality is supported for multiple GPU execution.

Supported functionality:

- Plans operating on two or four GPUs are supported.
- ► Three GPUs are supported for 2D and 3D transforms or when number of batches is greater than 1.
- ▶ All GPUs must have the same CUDA architecture level.
- ► The GPUs must support the Unified Virtual Address Space.
- On Windows, the GPU boards must be operating in Tesla Compute Cluster (TCC) mode.
- Running cuFFT on multiple GPUs is not compatible with an application that uses the CUDA Driver API.
- Strided input and output are not supported.
- ▶ When the number of batches is 1:
 - ▶ Only **c2c** and **z2z** transform types are supported.
 - Only in-place transforms are supported.
 - ▶ For 1D transforms, the dimension must be a power of 2.
 - ► For 2D and 3D transforms, the dimensions must factor into primes less than or equal to 127.
 - The X and Y dimensions of the transform must be greater than or equal to 64.

General guidelines are:

- ► The data for the entire transform must fit within the memory of the GPUs assigned to it.
- For batch size m on n GPUs:
 - The first **m** % **n** GPUs execute $\left[\frac{\mathbf{m}}{\mathbf{n}} \right] + 1$ transforms.
 - The remaining GPUs execute $\left[\left[\frac{m}{n} \right] \right]$ transforms.

Batch size output differences:

Single GPU cuFFT results are always returned in natural order. When multiple GPUs are used to perform more than one transform, the results are also returned in natural order. When multiple GPUs are used to perform a single transform the results are returned in a permutation of the normal results to reduce communication time.

Number of GPUs Number of transforms		Output Order on GPUs
One One or multiple transforms Natural order		Natural order
Multiple One Permuted results		Permuted results
Multiple	Multiple	Natural order

To produce natural order results in GPU memory in the 1D single transform case, requires calling **cufftXtMemcpy()** with **CUFFT_COPY_DEVICE_TO_DEVICE**.

2D and 3D transforms support execution of a transform given permuted order results as input. After execution in this case, the output will be in natural order. It is also possible to use **cufftxtMemcpy()** with **CUFFT_COPY_DEVICE_TO_DEVICE** to return 2D or 3D data to natural order.

NOTE:To create a cuFFT plan that runs on 4 GPUs, or on a pair of GPUs on different boards, requires a current license. Free evaluation licenses are available for registered developers until 12/31/2015. To learn more please visit the cuFFT developer page.

A license key can be set up as follows:

- ▶ Download the license key file (with extension .lic) to your machine.
- ▶ Set the environment variable LM_LICENSE_FILE to point to this license key.
- ▶ If the LM_LICENSE_FILE variable is already in use, you can simply append the path to your license key file to it. Alternatively, you can use the variable NVIDIA_LICENSE_FILE in place of LM_LICENSE_FILE.
- You can rename the license key file if you choose, but please make sure the .lic extension remains.

The end date for a license key file is mentioned in clear text in the license key.

The only supported multiple GPU configurations are 2 or 4 GPUs, all with the same CUDA architecture level. During the evaluation period, and if a license file is present, cuFFT will not check number of GPUs or architecture level in the cufftXt APIs.

See the cuFFT Code Examples section for single GPU and multiple GPU examples.

2.9. cuFFT Callback Routines

Callback routines are user-supplied kernel routines that cuFFT will call when loading or storing data. They allow the user to do data pre- or post- processing without additional kernel calls.

2.9.1. Overview of the cufFFT Callback Routine Feature

cuFFT provides a set of APIs that allow the cuFFT user to provide CUDA functions that re-direct or manipulate the data as it is loaded prior to processing the FFT, or stored once the FFT has been done. For the load callback, cuFFT passes the callback routine the address of the input data and the offset to the value to be loaded from device memory, and the callback routine returns the value it wishes cuFFT to use instead. For the store callback, cufFFT passes the callback routine the value it has computed, along with the

address of the output data and the offset to the value to be written to device memory, and the callback routine modifies the value and stores the modified result.

In order to provide a callback to cuFFT, a plan is created and configured normally using the extensible plan APIs. After the call to cufftCreate and cufftMakePlan, the user may associate a load callback routine, or a store callback routine, or both, with the plan, by callingcufftXtSetCallback. The caller also has the option to specify a device pointer to an opaque structure they wish to associate with the plan. This pointer will be passed to the callback routine by the cuFFT library. The caller may use this structure to remember plan dimensions and strides, or have a pointer to auxiliary data, etc.

With some restrictions, the callback routine is allowed to request shared memory for its own use. If the requested amount of shared memory is available, cufft will pass a pointer to it when it calls the callback routine.

CUFFT allows for 8 types of callback routine, one for each possible combination of: load or store, real or complex, single precision or double. It is the caller's responsibility to provide a routine that matches the function prototype for the type of routine specified. If there is already a callback of the specified type associated with the plan, the set callback function will replace it with the new one.

The callback routine extensions to cuFFT are built on the extensible cuFFT API. The general steps in defining and executing a transform with callbacks are:

- cufftCreate() create an empty plan, as in the single GPU case
- **cufftMakePlan{1d,2d,3d,Many}()** create the plan. These are the same functions used in the single GPU case.
- cufftXtSetCallback() called for load and/or store callback for this plan
- cufftExecC2C() etc. execute the plan
- cufftDestroy() free cuFFT plan resources

Callback functions are not supported on transforms with a dimension size that does not factor into primes smaller than 127. Callback functions on plans whose dimensions' prime factors are limited to 2, 3, 5, and 7 can safely call __syncthreads(). On other plans, results are not defined.

NOTE:The callback API is available in the statically linked cuFFT library only, and only on 64 bit LINUX operating systems.

2.9.2. Specifying Load and Store Callback Routines

In order to associate a callback routine with a plan, it is necessary to obtain a device pointer to the callback routine.

As an example, if the user wants to specify a load callback for an R2C transform, they would write the device code for the callback function, and define a global device variable that contains a pointer to the function:

From the host side, the user then has to get the address of the callback routine, which is stored in myOwnCallbackPtr. This is done with cudaMemcpyFromSymbol, as follows:

hostCopyOfCallbackPtr then contains the device address of the callback routine, that should be passed to cufftXtSetCallback. Note that, for multi-GPU transforms, hostCopyOfCallbackPtr will need to be an array of pointers, and the cudaMemcpyFromSymbol will have to be invoked for each GPU.

2.9.3. Callback Routine Function Details

Below are the function prototypes, and typedefs for pointers to the user supplied callback routines that cuFFT calls to load data prior to the transform.

```
typedef cufftComplex (*cufftCallbackLoadC) (void *dataIn,
                                           size_t offset,
                                            void *callerInfo,
                                            void *sharedPointer);
typedef cufftDoubleComplex (*cufftCallbackLoadZ)(void *dataIn,
                                                   size_t offset,
                                                   void *callerInfo,
                                                   void *sharedPointer);
typedef cufftReal (*cufftCallbackLoadR) (void *dataIn,
                                  size_t offset,
                                         void *callerInfo,
                                         void *sharedPointer);
typedef cufftDoubleReal (*cufftCallbackLoadD)(void *dataIn,
                                                size_t offset,
                                                void *callerInfo,
                                                void *sharedPointer);
```

Parameters for all of the load callbacks are defined as below:

• **offset**: offset of the input element from the start of output data. This is not a byte offset, rather it is the number of elements from start of data.

- dataIn: device pointer to the start of the input array that was passed in the cufftExecute call.
- callerInfo: device pointer to the optional caller specified data passed in the cufftXtSetCallback call.
- sharedPointer: pointer to shared memory, valid only if the user has called cufftXtSetCallbackSharedSize().

Below are the function prototypes, and typedefs for pointers to the user supplied callback routines that cuFFT calls to store data after completion of the transform. Note that the store callback functions do not return a value. This is because a store callback function is responsible not only for transforming the data as desired, but also for writing the data to the desired location. This allows the store callback to rearrange the data, for example to shift the zero frequency result to the center of the ouput.

```
typedef void (*cufftCallbackStoreC) (void *dataOut,
                                     size t offset,
                                     cufftComplex element,
                                     void *callerInfo,
                                     void *sharedPointer);
typedef void (*cufftCallbackStoreZ) (void *dataOut,
                                    size t offset,
                                     cufftDoubleComplex element,
                                     void *callerInfo,
                                    void *sharedPointer);
typedef void (*cufftCallbackStoreR) (void *dataOut,
                                     size t offset,
                                     cufftReal element,
                                     void *callerInfo,
                                     void *sharedPointer);
typedef void (*cufftCallbackStoreD) (void *dataOut,
                                    size t offset,
                                    cufftDoubleReal element,
                                     void *callerInfo,
                                    void *sharedPointer);
```

Parameters for all of the store callbacks are defined as below:

- **offset**: offset of the output element from the start of output data. This is not a byte offset, rather it is the number of elements from start of data.
- ▶ dataOut: device pointer to the start of the output array that was passed in the cufftExecute call.
- **element**: the real or complex result computed by CUFFT for the element specified by the offset argument.
- callerInfo: device pointer to the optional caller specified data passed in the cufftXtSetCallback call.
- sharedPointer: pointer to shared memory, valid only if the user has called cufftXtSetCallbackSharedSize().

2.9.4. Coding Considerations for the cuFFT Callback Routine Feature

cuFFT supports callbacks on all types of transforms, regardless of precision, dimension, batch, stride between elements, or number of GPUs.

cuFFT supports a wide range of parameters, and based on those for a given plan, it attempts to optimize performance. The number of kernels launched, and for each of those, the number of blocks launched and the number of threads per block, will vary depending on how cuFFT decomposes the transform. For some configurations, cuFFT will load or store (and process) multiple inputs or outputs per thread. For some configurations, threads may load or store inputs or outputs in any order, and cuFFT does not guarantee that the inputs or outputs handled by a given thread will be contiguous. These characteristics may vary with transform size, transform type (e.g. C2C vs C2R), number of dimensions, and GPU architecture. These variations may also change from one library version to the next.

cuFFT will call the load callback routine, for each point in the input, once and only once. Similarly it will call the store callback routine, for each point in the output, once and only once. If cuFFT is implementing a given FFT in multiple phases, it will only call the load callback routine from the first phase kernel(s), and it will only call the store callback routine from the last phase kernel(s).

When cufft is using only a single kernel, both the load and store callback routines will be called from the same kernel. In this case, if the transform is being done in-place (i.e. input data and output data are in the same memory location) the store callback can not safely write outside the confines of the specified element, unless it is writing the data to a completley separate output buffer.

When more than one kernel are used to implement a transform, the thread and block structure of the first kernel (the one that does the load) is often different from the thread and block structure of the last kernel (the one that does the store)

For multi-GPU transforms, the index passed to the callback routine is the element index from the start of data *on that GPU*, not from the start of the entire input or output data array.

For transforms whose dimensions can be factored into powers of 2, 3, 5, or 7, cuFFT guarantees that it will call the load and store callback routines from points in the kernel at which the code has converged (all threads in any given block will invoke the callback routine). This allows the callback routine to invoke __syncthreads internally as needed. Of course the caller is responsible for guaranteeing that the callback routine is at a point where the callback code has converged, to avoid deadlock. For plans whose dimensions are factored into higher primes, results of a callback routine calling syncthreads are not defined.

2.10. Thread Safety

cuFFT APIs are thread safe as long as different host threads execute FFTs using different plans and the output data are disjoint.

2.11. Static Library and Callback Support

Starting with release 6.5, the cuFFT Libraries are also delivered in a static form as libcufft_static.a and libcufftw_static.a on Linux and Mac and as cufft_static.lib. Static libraries are not supported on Windows. The static cufft and cufftw libraries depend on thread abstraction layer library libculibos.a.

For example, on linux, to compile a small application using cuFFT against the dynamic library, the following command can be used:

```
nvcc myCufftApp.c -lcufft -o myCufftApp
```

For cufftw on Linux, to compile a small application against the dynamic library, the following command can be used:

```
nvcc myCufftwApp.c -lcufftw -lcufft -o myCufftwApp
```

Whereas to compile against the static cuFFT library, the following command has to be used:

```
nvcc myCufftApp.c -lcufft_static -lculibos -o myCufftApp
```

Similarly to compile against the static cufftw library, the following command has to be used:

```
nvcc myCufftwApp.c libcufftw_static.a libcufft_static.a libculibos.a
-o myCufftwApp
```

It is also possible to use the native Host C++ compiler. Depending on the Host Operating system, some additional libraries like **pthread** or **d1** might be needed on the linking line. The following command on Linux is suggested:

```
g++ myCufftApp.c -lcufft_static -lculibos -lcudart_static -lpthread -ldl
-I <cuda-toolkit-path>/include -L <cuda-toolkit-path>/lib64 -o myCufftApp
```

Note that in the latter case, the library **cuda** is not needed. The CUDA Runtime will try to open explicitly the **cuda** library if needed. In the case of a system which does not have the CUDA driver installed, this allows the application to gracefully manage this issue and potentially run if a CPU-only path is available.

An application can be built with the cuFFT static library that will run on any CUDA hardware with SM20 or above. However cuFFT is not built with code for all possible SMs. Some kernels are built only on select architectures. This can cause warnings at link time that architectures are missing from these kernels. These warnings can safely be ignored.

On 64 bit LINUX operating systems, the cuFFT static library supports user supplied callback routines. The callback routines are CUDA device code, and must be separately compiled with NVCC and linked with the cuFFT library. Refer to the NVCC documentation regarding separate compilation for details. If you specify an SM when compiling your callback functions, you must specify one of the SM's cuFFT includes. On X86 platforms, these are SM20, SM30, SM35, and SM50. On Arm, cuFFT is built for SM32 only.

2.12. Accuracy and Performance

A DFT can be implemented as a matrix vector multiplication that requires $O(N^2)$ operations. However, the cuFFT Library employs the Cooley-Tukey algorithm to reduce the number of required operations to optimize the performance of particular transform sizes. This algorithm expresses the DFT matrix as a product of sparse building block matrices. The cuFFT Library implements the following building blocks: radix-2, radix-3, radix-5, and radix-7. Hence the performance of any transform size that can be factored as $2^a \times 3^b \times 5^c \times 7^d$ (where a, b, c, and d are non-negative integers) is optimized in the cuFFT library. There are also radix-m building blocks for other primes, m, whose value is < 128. When the length cannot be decomposed as multiples of powers of primes from 2 to 127, Bluestein's algorithm is used. Since the Bluestein implementation requires more computations per output point than the Cooley-Tukey implementation, the accuracy of the Cooley-Tukey algorithm is better. The pure Cooley-Tukey implementation has excellent accuracy, with the relative error growing proportionally to $\log_2(N)$, where N is the transform size in points.

For sizes handled by the Cooley-Tukey code path, the most efficient implementation is obtained by applying the following constraints (listed in order from the most generic to the most specialized constraint, with each subsequent constraint providing the potential of an additional performance improvement).

Applies to	Recommendation	Comment
All	Use single precision transforms.	Single precision transforms require less bandwidth per computation than double precision transforms.
All	Restrict the size along all dimensions to be representable as $2^a \times 3^b \times 5^c \times 7^d$.	The cuFFT library has highly optimized kernels for transforms whose dimensions have these prime factors. In general the best performance occurs when using powers of 2, followed by powers of 3, then 5, 7.
All	Restrict the size along each dimension to use fewer distinct prime factors.	A transform of size 2^n or 3^n will usually be faster than one of size $2^i \times 3^j$ even if the latter is slightly smaller, due to the composition of specialized paths.
All	Restrict the data to be contiguous in memory when performing a single	The cuFFT library has been optimized for this data layout.

Applies to	Recommendation	Comment
	transform. When performing multiple transforms make the individual datasets contiguous	
All	Perform multiple (i.e., batched) transforms. Additional optimizations are performed in batched mode.	
		This scheme uses more efficient kernels to implement conjugate symmetry property.
real-to-complex transforms or complex- to-real transforms	forms or complex- kernels than in-place mode.	
Multiple GPU transforms Use PCI Express 3.0 between GPUs and ensure the GPUs are on the same switch. The faster the interconnect between the GPUs, the faster performance.		between the GPUs, the faster the

Chapter 3. CUFFT API REFERENCE

This chapter specifies the behavior of the cuFFT library functions by describing their input/output parameters, data types, and error codes. The cuFFT library is initialized upon the first invocation of an API function, and cuFFT shuts down automatically when all user-created FFT plans are destroyed.

3.1. Return value cufftResult

All cuFFT Library return values except for **CUFFT_SUCCESS** indicate that the current API call failed and the user should reconfigure to correct the problem. The possible return values are defined as follows:

```
typedef enum cufftResult_t {
    CUFFT_SUCCESS = 0, // The cuFFT operation was successful
    CUFFT_INVALID_PLAN = 1, // cuFFT was passed an invalid plan handle
    CUFFT_ALLOC_FAILED = 2, // cuFFT failed to allocate GPU or CPU memory
    CUFFT_INVALID_TYPE = 3, // No longer used
    CUFFT_INVALID_VALUE = 4, // User specified an invalid pointer or

parameter
    CUFFT_INTERNAL_ERROR = 5, // Driver or internal cuFFT library error
    CUFFT_EXEC_FAILED = 6, // Failed to execute an FFT on the GPU
    CUFFT_SETUP_FAILED = 7, // The cuFFT library failed to initialize
    CUFFT_INVALID_SIZE = 8, // User specified an invalid transform size
    CUFFT_UNALIGNED_DATA = 9, // No longer used
    CUFFT_INCOMPLETE_PARAMETER_LIST = 10, // Missing parameters in call
    CUFFT_INVALID_DEVICE = 11, // Execution of a plan was on different GPU than
plan creation
    CUFFT_PARSE_ERROR = 12, // Internal plan database error
    CUFFT_NO_WORKSPACE = 13 // No workspace has been provided prior to plan
execution
} cufftResult;
```

Users are encouraged to check return values from cuFFT functions for errors as shown in cuFFT Code Examples.

3.2. cuFFT Basic Plans

3.2.1. Function cufftPlan1d()

```
cufftResult
    cufftPlan1d(cufftHandle *plan, int nx, cufftType type, int batch);
```

Creates a 1D FFT plan configuration for a specified signal size and data type. The **batch** input parameter tells cuFFT how many 1D transforms to configure.

Input

plan	Pointer to a cufftHandle object	
nx	The transform size (e.g. 256 for a 256-point FFT)	
type	The transform data type (e.g., CUFFT_C2C for single precision complex to complex)	
batch	Number of transforms of size nx. Deprecated - use cufftPlanMany for multiple transforms.	

Output

plan	Contains a cuFFT 1D plan handle value
------	---------------------------------------

Return Values

CUFFT_SUCCESS	cuFFT successfully created the FFT plan.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	The nx or batch parameter is not a supported size.

3.2.2. Function cufftPlan2d()

```
cufftResult
  cufftPlan2d(cufftHandle *plan, int nx, int ny, cufftType type);
```

Creates a 2D FFT plan configuration according to specified signal sizes and data type.

Input

plan	Pointer to a cufftHandle object
nx	The transform size in the x dimension (number of rows)
ny	The transform size in the y dimension (number of columns)
type	The transform data type (e.g., CUFFT_C2R for single precision complex to real)

Output

olan	Contains a cuFFT 2D plan handle value
------	---------------------------------------

Return Values

CUFFT_SUCCESS	cuFFT successfully created the FFT plan.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	Either or both of the nx or ny parameters is not a supported size.

3.2.3. Function cufftPlan3d()

```
cufftResult
  cufftPlan3d(cufftHandle *plan, int nx, int ny, int nz, cufftType type);
```

Creates a 3D FFT plan configuration according to specified signal sizes and data type. This function is the same as **cufftPlan2d()** except that it takes a third size parameter **nz**.

Input

plan	Pointer to a cufftHandle object
nx	The transform size in the x dimension
ny	The transform size in the y dimension
nz	The transform size in the z dimension
type	The transform data type (e.g., CUFFT_R2C for single precision real to complex)

Output

olan	Contains a cuFFT 3D plan handle value
------	---------------------------------------

Return Values

CUFFT_SUCCESS	cuFFT successfully created the FFT plan.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	One or more of the nx, ny, or nz parameters is not a supported size.

3.2.4. Function cufftPlanMany()

```
cufftResult
  cufftPlanMany(cufftHandle *plan, int rank, int *n, int *inembed,
        int istride, int idist, int *onembed, int ostride,
        int odist, cufftType type, int batch);
```

Creates a FFT plan configuration of dimension **rank**, with sizes specified in the array **n**. The **batch** input parameter tells cuFFT how many transforms to configure. With this function, batched plans of 1, 2, or 3 dimensions may be created.

The **cufftPlanMany()** API supports more complicated input and output data layouts via the advanced data layout parameters: **inembed**, **istride**, **idist**, **onembed**, **ostride**, and **odist**.

If **inembed** and **onembed** are set to **NULL**, all other stride information is ignored, and default strides are used. The default assumes contiguous data arrays.

All arrays are assumed to be in CPU memory.

Input

plan	Pointer to a cufftHandle object
rank	Dimensionality of the transform (1, 2, or 3)
n	Array of size rank, describing the size of each dimension
inembed	Pointer of size rank that indicates the storage dimensions of the input data in memory. If set to NULL all other advanced data layout parameters are ignored.
istride	Indicates the distance between two successive input elements in the least significant (i.e., innermost) dimension
idist	Indicates the distance between the first element of two consecutive signals in a batch of the input data
onembed	Pointer of size rank that indicates the storage dimensions of the output data in memory. If set to NULL all other advanced data layout parameters are ignored.
ostride	Indicates the distance between two successive output elements in the output array in the least significant (i.e., innermost) dimension
odist	Indicates the distance between the first element of two consecutive signals in a batch of the output data
type	The transform data type (e.g., CUFFT_R2C for single precision real to complex)
batch	Batch size for this transform

Output

plan	Contains a cuFFT plan handle
------	------------------------------

Return Values

CUFFT_SUCCESS	cuFFT successfully created the FFT plan.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	One or more of the parameters is not a supported size.

3.3. cuFFT Extensible Plans

This API separates handle creation from plan generation. This makes it possible to change plan settings, which may alter the outcome of the plan generation phase, before the plan is actually generated.

3.3.1. Function cufftCreate()

```
cufftResult
  cufftCreate(cufftHandle *plan);
```

Creates only an opaque handle, and allocates small data structures on the host. The cufftMakePlan*() calls actually do the plan generation. It is recommended that cufftSet*() calls, such as cufftSetCompatibilityMode(), that may require a plan to be broken down and re-generated, should be made after cufftCreate() and before one of the cufftMakePlan*() calls.

Input

plan	Pointer to a cufftHandle object
Output	
plan	Contains a cuFFT plan handle value

Return Values

CUFFT_SUCCESS	cuFFT successfully created the FFT plan.
CUFFT_ALLOC_FAILED	The allocation of resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.

3.3.2. Function cufftMakePlan1d()

Following a call to **cufftCreate()** makes a 1D FFT plan configuration for a specified signal size and data type. The **batch** input parameter tells cuFFT how many 1D transforms to configure.

If cufftXtSetGPUs () was called prior to this call with multiple GPUs, then workSize will contain multiple sizes. See sections on multiple GPUs for more details.

Input

plan	cufftHandle returned by cufftCreate

nx	The transform size (e.g. 256 for a 256-point FFT). For multiple GPUs, this must be a power of 2.
type	The transform data type (e.g., CUFFT_C2C for single precision complex to complex). For multiple GPUs this must be a complex to complex transform.
batch	Number of transforms of size nx. Deprecated - use cufftMakePlanMany for multiple transforms.
*workSize	Pointer to the size(s) of the work areas. For example for two GPUs worksize must be declared to have two elements.

Output

*workSize	Pointer to the size(s) of the work areas.
-----------	---

Return Values

CUFFT_SUCCESS	cuFFT successfully created the FFT plan.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle. Handle is not valid when multi-GPU restrictions are not met.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	The nx or batch parameter is not a supported size.

3.3.3. Function cufftMakePlan2d()

Following a call to **cufftCreate()** makes a 2D FFT plan configuration according to specified signal sizes and data type.

If cufftXtSetGPUs () was called prior to this call with multiple GPUs, then workSize will contain multiple sizes. See sections on multiple GPUs for more details.

Input

plan	cufftHandle returned by cufftCreate
nx	The transform size in the x dimension (number of rows). For multiple GPUs, this must be factorable into primes less than or equal to 127.
ny	The transform size in the y dimension (number of columns). For 2 GPUs, this must be factorable into primes less than or equal to 127.
type	The transform data type (e.g., CUFFT_C2R for single precision complex to real). For multiple GPUs this must be a complex to complex transform.

*workSize	Pointer to the size(s) of the work areas. For example for two
	GPUs worksize must be declared to have two elements.

Output

*workSize	Pointer to the size(s) of the work areas.
-----------	---

Return Values

CUFFT_SUCCESS	cuFFT successfully created the FFT plan.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	Either or both of the nx or ny parameters is not a supported size.

3.3.4. Function cufftMakePlan3d()

Following a call to **cufftCreate()** makes a 3D FFT plan configuration according to specified signal sizes and data type. This function is the same as **cufftPlan2d()** except that it takes a third size parameter **nz**.

If cufftXtSetGPUs () was called prior to this call with multiple GPUs, then workSize will contain multiple sizes. See sections on multiple GPUs for more details.

Input

plan	cufftHandle returned by cufftCreate
nx	The transform size in the x dimension. For multiple GPUs, this must be factorable into primes less than or equal to 127.
ny	The transform size in the y dimension. For multiple GPUs, this must be factorable into primes less than or equal to 127.
nz	The transform size in the z dimension. For multiple GPUs, this must be factorable into primes less than or equal to 127.
type	The transform data type (e.g., CUFFT_R2C for single precision real to complex). For multiple GPUs this must be a complex to complex transform.
*workSize	Pointer to the size(s) of the work areas. For example for two GPUs worksize must be declared to have two elements.

Output

*workSize

Return Values

CUFFT_SUCCESS	cuFFT successfully created the FFT plan.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	One or more of the nx, ny, or nz parameters is not a supported size.

3.3.5. Function cufftMakePlanMany()

```
cufftResult
  cufftMakePlanMany(cufftHandle plan, int rank, int *n, int *inembed,
        int istride, int idist, int *onembed, int ostride,
        int odist, cufftType type, int batch, size t *workSize);
```

Following a call to **cufftCreate()** makes a FFT plan configuration of dimension **rank**, with sizes specified in the array **n**. The **batch** input parameter tells cuFFT how many transforms to configure. With this function, batched plans of 1, 2, or 3 dimensions may be created.

The **cufftPlanMany()** API supports more complicated input and output data layouts via the advanced data layout parameters: **inembed**, **istride**, **idist**, **onembed**, **ostride**, and **odist**.

If **inembed** and **onembed** are set to **NULL**, all other stride information is ignored, and default strides are used. The default assumes contiguous data arrays.

If **cufftXtSetGPUs()** was called prior to this call with multiple GPUs, then **workSize** will contain multiple sizes. See sections on multiple GPUs for more details.

All arrays are assumed to be in CPU memory.

Input

plan	cufftHandle returned by cufftCreate
rank	Dimensionality of the transform (1, 2, or 3)
n	Array of size rank, describing the size of each dimension. For multiple GPUs and rank equal to 1, the sizes must be a power of 2. For multiple GPUs and rank equal to 2 or 3, the sizes must be factorable into primes less than or equal to 127.
inembed	Pointer of size rank that indicates the storage dimensions of the input data in memory. If set to NULL all other advanced data layout parameters are ignored.
istride	Indicates the distance between two successive input elements in the least significant (i.e., innermost) dimension
idist	Indicates the distance between the first element of two consecutive signals in a batch of the input data

onembed	Pointer of size rank that indicates the storage dimensions of the output data in memory. If set to NULL all other advanced data layout parameters are ignored.
ostride	Indicates the distance between two successive output elements in the output array in the least significant (i.e., innermost) dimension
odist	Indicates the distance between the first element of two consecutive signals in a batch of the output data
type	The transform data type (e.g., CUFFT_R2C for single precision real to complex). For 2 GPUs this must be a complex to complex transform.
batch	Batch size for this transform
*workSize	Pointer to the size(s) of the work areas. For example for two GPUs worksize must be declared to have two elements.

Output

*workSize	Pointer to the size(s) of the work areas.
-----------	---

Return Values

CUFFT_SUCCESS	cuFFT successfully created the FFT plan.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle. Handle is not valid when multi-GPU restrictions are not met.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	One or more of the parameters is not a supported size.

3.4. cuFFT Estimated Size of Work Area

During plan execution, cuFFT requires a work area for temporary storage of intermediate results. The cufftEstimate*() calls return an estimate for the size of the work area required, given the specified parameters, and assuming default plan settings. Some problem sizes require much more storage than others. In particular powers of 2 are very efficient in terms of temporary storage. Large prime numbers, however, use different algorithms and may need up to the eight times that of a similarly sized power of 2. These routines return estimated workSize values which may still be smaller than the actual values needed especially for values of n that are not multiples of powers of 2, 3, 5 and 7. More refined values are given by the cufftGetSize*() routines, but these values may still be conservative.

3.4.1. Function cufftEstimate1d()

```
cufftResult
  cufftEstimateld(int nx, cufftType type, int batch, size_t *workSize);
```

During plan execution, cuFFT requires a work area for temporary storage of intermediate results. This call returns an estimate for the size of the work area required, given the specified parameters, and assuming default plan settings. Note that changing some plan settings, such as compatibility mode, may alter the size required for the work area.

Input

nx	The transform size (e.g. 256 for a 256-point FFT)
type	The transform data type (e.g., CUFFT_C2C for single precision complex to complex)
batch	Number of transforms of size nx. Deprecated - use cufftEstimateMany for multiple transforms.
*workSize	Pointer to the size of the work space.

Output

*workSize	Pointer to the size of the work space
-----------	---------------------------------------

Return Values

CUFFT_SUCCESS	cuFFT successfully returned the size of the work space.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	The nx parameter is not a supported size.

3.4.2. Function cufftEstimate2d()

```
cufftResult
   cufftEstimate2d(int nx, int ny, cufftType type, size_t *workSize);
```

During plan execution, cuFFT requires a work area for temporary storage of intermediate results. This call returns an estimate for the size of the work area required, given the specified parameters, and assuming default plan settings. Note that changing some plan settings, such as compatibility mode, may alter the size required for the work area.

Input

nx	The transform size in the x dimension (number of rows)
ny	The transform size in the y dimension (number of columns)

type	The transform data type (e.g., CUFFT_C2R for single precision complex to real)
*workSize	Pointer to the size of the work space.

Output

workSize	Pointer to the size of the work space
----------	---------------------------------------

Return Values

CUFFT_SUCCESS	cuFFT successfully returned the size of the work space.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	Either or both of the nx or ny parameters is not a supported size.

3.4.3. Function cufftEstimate3d()

```
cufftResult
   cufftEstimate3d(int nx, int ny, int nz, cufftType type, size t *workSize);
```

During plan execution, cuFFT requires a work area for temporary storage of intermediate results. This call returns an estimate for the size of the work area required, given the specified parameters, and assuming default plan settings. Note that changing some plan settings, such as compatibility mode, may alter the size required for the work area.

Input

nx	The transform size in the x dimension
ny	The transform size in the y dimension
nz	The transform size in the z dimension
type	The transform data type (e.g., CUFFT_R2C for single precision real to complex)
*workSize	Pointer to the size of the work space.

Output

*workSize	Pointer to the size of the work space
-----------	---------------------------------------

Return Values

CUFFT_SUCCESS	cuFFT successfully returned the size of the work space.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.

CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	One or more of the nx, ny, or nz parameters is not a supported size.

3.4.4. Function cufftEstimateMany()

```
cufftResult
  cufftEstimateMany(int rank, int *n, int *inembed,
        int istride, int idist, int *onembed, int ostride,
        int odist, cufftType type, int batch, size_t *workSize);
```

During plan execution, cuFFT requires a work area for temporary storage of intermediate results. This call returns an estimate for the size of the work area required, given the specified parameters, and assuming default plan settings. Note that changing some plan settings, such as compatibility mode, may alter the size required for the work area.

The **cufftEstimateMany()** API supports more complicated input and output data layouts via the advanced data layout parameters: **inembed**, **istride**, **idist**, **onembed**, **ostride**, and **odist**.

All arrays are assumed to be in CPU memory.

Input

rank	Dimensionality of the transform (1, 2, or 3)
n	Array of size rank, describing the size of each dimension
inembed	Pointer of size rank that indicates the storage dimensions of the input data in memory. If set to NULL all other advanced data layout parameters are ignored.
istride	Indicates the distance between two successive input elements in the least significant (i.e., innermost) dimension
idist	Indicates the distance between the first element of two consecutive signals in a batch of the input data
onembed	Pointer of size rank that indicates the storage dimensions of the output data in memory. If set to NULL all other advanced data layout parameters are ignored.
ostride	Indicates the distance between two successive output elements in the output array in the least significant (i.e., innermost) dimension
odist	Indicates the distance between the first element of two consecutive signals in a batch of the output data
type	The transform data type (e.g., CUFFT_R2C for single precision real to complex)
batch	Batch size for this transform
*workSize	Pointer to the size of the work space.

Output

*workSize	Pointer to the size of the work space
-----------	---------------------------------------

Return Values

CUFFT_SUCCESS	cuFFT successfully returned the size of the work space.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	One or more of the parameters is not a supported size.

3.5. cuFFT Refined Estimated Size of Work Area

The **cufftGetSize*()** routines give a more accurate estimate of the work area size required for a plan than the **cufftEstimate*()** routines as they take into account any plan settings that may have been made. As discussed in the section cuFFT Estimated Size of Work Area, the **workSize** value(s) returned may be conservative especially for values of **n** that are not multiples of powers of 2, 3, 5 and 7.

3.5.1. Function cufftGetSize1d()

This call gives a more accurate estimate of the work area size required for a plan than **cufftEstimateld()**, given the specified parameters, and taking into account any plan settings that may have been made.

Input

plan	cufftHandle returned by cufftCreate
nx	The transform size (e.g. 256 for a 256-point FFT)
type	The transform data type (e.g., cufft_c2c for single precision complex to complex)
batch	Number of transforms of size nx. Deprecated - use cufftGetSizeMany for multiple transforms.
*workSize	Pointer to the size of the work space. For example for two GPUs worksize must be declared to have two elements.

Output

*workSize	Pointer to the size of the work space
-----------	---------------------------------------

CUFFT_SUCCESS	cuFFT successfully returned the size of the work space.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.

CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	The nx parameter is not a supported size.

3.5.2. Function cufftGetSize2d()

This call gives a more accurate estimate of the work area size required for a plan than **cufftEstimate2d()**, given the specified parameters, and taking into account any plan settings that may have been made.

Input

plan	cufftHandle returned by cufftCreate
nx	The transform size in the x dimension (number of rows)
ny	The transform size in the y dimension (number of columns)
type	The transform data type (e.g., CUFFT_C2R for single precision complex to real)
*workSize	Pointer to the size of the work space. For example for two GPUs worksize must be declared to have two elements.

Output

*workSize	Pointer to the size of the work space
-----------	---------------------------------------

Return Values

CUFFT_SUCCESS	cuFFT successfully returned the size of the work space.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	Either or both of the nx or ny parameters is not a supported size.

3.5.3. Function cufftGetSize3d()

This call gives a more accurate estimate of the work area size required for a plan than <code>cufftEstimate3d()</code>, given the specified parameters, and taking into account any plan settings that may have been made.

Input

plan	cufftHandle returned by cufftCreate
nx	The transform size in the x dimension
ny	The transform size in the y dimension
nz	The transform size in the z dimension
type	The transform data type (e.g., CUFFT_R2c for single precision real to complex)
*workSize	Pointer to the size of the work space. For example for two GPUs worksize must be declared to have two elements.

Output

*workSize	Pointer to the size of the work space.
	To the control of the state of

Return Values

CUFFT_SUCCESS	cuFFT successfully returned the size of the work space.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	One or more of the nx, ny, or nz parameters is not a supported size.

3.5.4. Function cufftGetSizeMany()

```
cufftResult
    cufftGetSizeMany(cufftHandle plan, int rank, int *n, int *inembed,
        int istride, int idist, int *onembed, int ostride,
        int odist, cufftType type, int batch, size_t *workSize);
```

This call gives a more accurate estimate of the work area size required for a plan than **cufftEstimateSizeMany()**, given the specified parameters, and taking into account any plan settings that may have been made.

Input

plan	cufftHandle returned by cufftCreate
rank	Dimensionality of the transform (1, 2, or 3)
n	Array of size rank, describing the size of each dimension
inembed	Pointer of size rank that indicates the storage dimensions of the input data in memory. If set to NULL all other advanced data layout parameters are ignored.

istride	Indicates the distance between two successive input elements in the least significant (i.e., innermost) dimension
idist	Indicates the distance between the first element of two consecutive signals in a batch of the input data
onembed	Pointer of size rank that indicates the storage dimensions of the output data in memory. If set to NULL all other advanced data layout parameters are ignored.
ostride	Indicates the distance between two successive output elements in the output array in the least significant (i.e., innermost) dimension
odist	Indicates the distance between the first element of two consecutive signals in a batch of the output data
type	The transform data type (e.g., CUFFT_R2c for single precision real to complex)
batch	Batch size for this transform
*workSize	Pointer to the size of the work space. For example for two GPUs worksize must be declared to have two elements.

Output

*workSize	Pointer to the size of the work area
-----------	--------------------------------------

Return Values

CUFFT_SUCCESS	cuFFT successfully returned the size of the work space.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_SIZE	One or more of the parameters is not a supported size.

3.6. Function cufftGetSize()

```
cufftResult
    cufftGetSize(cufftHandle plan, size_t *workSize);
```

Once plan generation has been done, either with the original API or the extensible API, this call returns the actual size of the work area required to support the plan. Callers who choose to manage work area allocation within their application must use this call after plan generation, and after any cufftSet*() calls subsequent to plan generation, if those calls might alter the required work space size.

Input

*workSize	Pointer to the size of the work space. For example for two
	GPUs worksize must be declared to have two elements.

Output

*workSize	Pointer to the size of the work space
-----------	---------------------------------------

Return Values

CUFFT_SUCCESS	cuFFT successfully returned the size of the work space.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.

3.7. cuFFT Caller Allocated Work Area Support

3.7.1. Function cufftSetAutoAllocation()

```
cufftResult
  cufftSetAutoAllocation(cufftHandle plan, int autoAllocate);
```

cufftSetAutoAllocation() indicates that the caller intends to allocate and manage work areas for plans that have been generated. cuFFT default behavior is to allocate the work area at plan generation time. If cufftSetAutoAllocation() has been called with autoAllocate set to 0 ("false") prior to one of the cufftMakePlan*() calls, cuFFT does not allocate the work area. This is the preferred sequence for callers wishing to manage work area allocation.

Input

plan	cufftHandle returned by cufftCreate.
autoAllocate	Indicates whether to allocate work area.

Return Values

CUFFT_SUCCESS	cuFFT successfully allows user to manage work area.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.

3.7.2. Function cufftSetWorkArea()

```
cufftResult
  cufftSetWorkArea(cufftHandle plan, void *workArea);
```

cufftSetWorkArea() overrides the work area pointer associated with a plan.
If the work area was auto-allocated, cuFFT frees the auto-allocated space. The
cufftExecute*() calls assume that the work area pointer is valid and that it points to
a contiguous region in device memory that does not overlap with any other work area. If
this is not the case, results are indeterminate.

Input

plan	cufftHandle returned by cufftCreate
	Pointer to workArea. For multiple GPUs, multiple work area pointers must be given.

Return Values

CUFFT_SUCCESS	cuFFT successfully allows user to override workArea pointer.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.

3.8. Function cufftDestroy()

```
cufftResult
  cufftDestroy(cufftHandle plan);
```

Frees all GPU resources associated with a cuFFT plan and destroys the internal plan data structure. This function should be called once a plan is no longer needed, to avoid wasting GPU memory.

Input

plan	The cufftHandle object of the plan to be destroyed.
------	---

Return Values

CUFFT_SUCCESS	cuFFT successfully destroyed the FFT plan.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.

3.9. cuFFT Execution

3.9.1. Functions cufftExecC2C() and cufftExecZ2Z()

```
cufftResult
   cufftExecC2C(cufftHandle plan, cufftComplex *idata,
        cufftComplex *odata, int direction);
cufftResult
   cufftExecZ2Z(cufftHandle plan, cufftDoubleComplex *idata,
        cufftDoubleComplex *odata, int direction);
```

cufftExecC2C() (cufftExecZ2Z()) executes a single-precision (double-precision)
complex-to-complex transform plan in the transform direction as specified by
direction parameter. cuFFT uses the GPU memory pointed to by the idata parameter
as input data. This function stores the Fourier coefficients in the odata array. If idata
and odata are the same, this method does an in-place transform.

Input

plan	cufftHandle returned by cufftCreate
idata	Pointer to the complex input data (in GPU memory) to transform
odata	Pointer to the complex output data (in GPU memory)
direction	The transform direction: CUFFT_FORWARD OF CUFFT_INVERSE

Output

odata	Contains the complex Fourier coefficients
-------	---

Return Values

CUFFT_SUCCESS	cuFFT successfully executed the FFT plan.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_INVALID_VALUE	At least one of the parameters idata, odata, and direction is not valid.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_EXEC_FAILED	cuFFT failed to execute the transform on the GPU.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.

3.9.2. Functions cufftExecR2C() and cufftExecD2Z()

```
cufftResult
    cufftExecR2C(cufftHandle plan, cufftReal *idata, cufftComplex *odata);
cufftResult
    cufftExecD2Z(cufftHandle plan, cufftDoubleReal *idata, cufftDoubleComplex *odata);
```

cufftExecR2C() (cufftExecD2Z()) executes a single-precision (double-precision) real-to-complex, implicitly forward, cuFFT transform plan. cuFFT uses as input data the GPU memory pointed to by the idata parameter. This function stores the nonredundant Fourier coefficients in the odata array. Pointers to idata and odata are both required to be aligned to cufftComplex data type in single-precision transforms and cufftDoubleComplex data type in double-precision transforms. If idata and odata are the same, this method does an in-place transform. Note the data layout differences between in-place and out-of-place transforms as described in Parameter cufftType.

Input

plan	cufftHandle returned by cufftCreate
idata	Pointer to the real input data (in GPU memory) to transform
odata	Pointer to the complex output data (in GPU memory)

Output

odata	Contains the complex Fourier coefficients

CUFFT_SUCCESS	cuFFT successfully executed the FFT plan.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_INVALID_VALUE	At least one of the parameters idata and odata is not valid.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_EXEC_FAILED	cuFFT failed to execute the transform on the GPU.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.

3.9.3. Functions cufftExecC2R() and cufftExecZ2D()

```
cufftResult
   cufftExecC2R(cufftHandle plan, cufftComplex *idata, cufftReal *odata);
cufftResult
   cufftExecZ2D(cufftHandle plan, cufftComplex *idata, cufftReal *odata);
```

cufftExecC2R() (cufftExecZ2D()) executes a single-precision (double-precision)
complex-to-real, implicitly inverse, cuFFT transform plan. cuFFT uses as input data
the GPU memory pointed to by the idata parameter. The input array holds only the
nonredundant complex Fourier coefficients. This function stores the real output values
in the odata array. and pointers are both required to be aligned to cufftComplex data
type in single-precision transforms and cufftDoubleComplex type in double-precision
transforms. If idata and odata are the same, this method does an in-place transform.

Input

plan	cufftHandle returned by cufftCreate
idata	Pointer to the complex input data (in GPU memory) to transform
odata	Pointer to the real output data (in GPU memory)

Output

odata	Contains the real output data
Ouata	contains the real output data

Return Values

CUFFT_SUCCESS	cuFFT successfully executed the FFT plan.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_INVALID_VALUE	At least one of the parameters idata and odata is not valid.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_EXEC_FAILED	cuFFT failed to execute the transform on the GPU.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.

3.10. cuFFT and Multiple GPUs

3.10.1. Function cufftXtSetGPUs()

```
cufftResult
  cufftXtSetGPUs(cufftHandle plan, int nGPUs, int *whichGPUs);
```

cufftXtSetGPUs () indentifies which GPUs are to be used with the plan. As in the single GPU case **cufftCreate** () creates a plan and **cufftMakePlan*** () does the plan generation. This call will return an error if a non-default stream has been associated with the plan.

Note that the call to **cufftXtSetGPUs()** must occur after the call to **cufftCreate()** and prior to the call to **cufftMakePlan*()**.

Input

plan	cufftHandle returned by cufftCreate
nGPUs	Number of GPUs to use
whichGPUs	The GPUs to use

Return Values

CUFFT_SUCCESS	cuFFT successfully set the GPUs to use.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle, or a non-default stream has been associated with the plan.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_VALUE	The requested number of GPUs was less than 2.
CUFFT_INVALID_DEVICE	An invalid GPU index was specified.
CUFFT_LICENSE_ERROR	A license file is required for the requested configuration.

3.10.2. Function cufftXtSetWorkArea()

```
cufftResult
  cufftXtSetWorkArea(cufftHandle plan, void **workArea);
```

cufftXtSetWorkArea() overrides the work areas associated with a plan. If the work area was auto-allocated, cuFFT frees the auto-allocated space. The cufftXtExec*() calls assume that the work area is valid and that it points to a contiguous region in each device memory that does not overlap with any other work area. If this is not the case, results are indeterminate.

Input

plan	cufftHandle returned by cufftCreate
workArea	Pointer to the pointers to workArea

CUFFT_SUCCESS	cuFFT successfully allows user to override workArea pointer.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_DEVICE	A GPU associated with the plan could not be selected.

3.10.3. cuFFT Multiple GPU Execution

3.10.3.1. Functions cufftXtExecDescriptorC2C() and cufftXtExecDescriptorZ2Z()

```
cufftResult
   cufftXtExecDescriptorC2C(cufftHandle plan, cudaLibXtDesc *idata,
        cudaLibXtDesc *idata, int direction);
cufftResult
   cufftXtExecDescriptorZ2Z(cufftHandle plan, cudaLibXtDesc *idata,
        cudaLibXtDesc *idata, int direction);
```

cufftXtExecDescriptorC2C() (cufftXtExecDescriptorZ2Z()) executes a single-precision (double-precision) complex-to-complex transform plan in the transform direction as specified by direction parameter. cuFFT uses the GPU memory pointed to by cudaLibXtDesc *idata as input data. Since only in-place multiple GPU functionality is support, this function also stores the result in the cudaLibXtDesc *idata arrays.

Input

plan	cufftHandle returned by cufftCreate
idata	Pointer to the complex input data (in GPU memory) to transform
idata	Pointer to the complex output data (in GPU memory)
direction	The transform direction: CUFFT_FORWARD or CUFFT_INVERSE

Output

idata	Contains the complex Fourier coefficients
-------	---

CUFFT_SUCCESS	cuFFT successfully executed the FFT plan.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_INVALID_VALUE	At least one of the parameters idata and direction is not valid.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_EXEC_FAILED	cuFFT failed to execute the transform on the GPU.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_DEVICE	An invalid GPU index was specified in a descriptor.

3.10.4. Memory Allocation and Data Movement Functions

Multiple GPU cuFFT execution functions assume a certain data layout in terms of what input data has been copied to which GPUs prior to execution, and what output data resides in which GPUs post execution. The following functions assist in allocation, setup and retrieval of the data. They must be called after the call to cufftMakePlan*().

3.10.4.1. Function cufftXtMalloc()

cufftXtMalloc() allocates a descriptor, and all memory for data in GPUs associated with the plan, and returns a pointer to the descriptor. Note the descriptor contains an array of device pointers so that the application may preprocess or postprocess the data on the GPUs. The enumerated parameter cufftXtSubFormat_t indicates if the buffer will be used for input or output.

Input

plan	cufftHandle returned by cufftCreate
descriptor	Pointer to a pointer to a cudaLibXtDesc object
format	cufftXtSubFormat Value

Output

descriptor	Pointer to a pointer to a cudaLibXtDesc object
------------	--

CUFFT_SUCCESS	cuFFT successfully allows user to allocate descriptor and GPU memory.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle or it is not a multiple GPU plan.
CUFFT_ALLOC_FAILED	The allocation of GPU resources for the plan failed.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_DEVICE	An invalid GPU index was specified in the descriptor.

3.10.4.1.1. Parameter cufftXtSubFormat

cufftXtSubFormat_t is an enumerated type that indicates if the buffer will be used for input or output and the ordering of the data.

3.10.4.2. Function cufftXtFree()

```
cufftResult
  cufftXtFree(cudaLibXtDesc *descriptor);
```

cufftXtFree() frees the descriptor and all memory associated with it. The descriptor and memory must have been returned by a previous call to **cufftXtMalloc()**.

Input

descriptor	Pointer to a cudaLibXtDesc Object

Return Values

CUFFT_SUCCESS	cuFFT successfully allows user to free descriptor and associated GPU memory.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.

3.10.4.3. Function cufftXtMemcpy()

```
cufftResult
  cufftXtMemcpy(cufftHandle plan, void *dstPointer, void *srcPointer,
       cufftXtCopyType type);
```

cufftXtMemcpy () copies data between buffers on the host and GPUs or between GPUs. The enumerated parameter **cufftXtCopyType_t** indicates the type and direction of transfer.

Input

plan	cufftHandle returned by cufftCreate
dstPointer	Pointer to the destination address(es)
srcPointer	Pointer to the source address(es)
type	cufftXtCopyTypeValue

CUFFT_SUCCESS	cuFFT successfully allows user to copy memory between host and GPUs or between GPUs.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_INVALID_VALUE	One or more invalid parameters were passed to the API.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.
CUFFT_INVALID_DEVICE	An invalid GPU index was specified in a descriptor.

3.10.4.3.1. Parameter cufftXtCopyType

cufftXtCopyType_t is an enumerated type for multiple GPU functions that specifies the type of copy for **cufftXtMemcpy()**.

CUFFT_COPY_HOST_TO_DEVICE copies data from a contiguous host buffer to multiple device buffers, in the layout cuFFT requires for input data. **dstPointer** must point to a **cudaLibXtDesc** structure, and **srcPointer** must point to a host memory buffer.

CUFFT_COPY_DEVICE_TO_HOST copies data from multiple device buffers, in the layout cuFFT produces for output data, to a contiguous host buffer. **dstPointer** must point to a host memory buffer, and **srcPointer** must point to a **cudalibXtDesc** structure.

CUFFT_COPY_DEVICE_TO_DEVICE copies data from multiple device buffers, in the layout cuFFT produces for output data, to multiple device buffers, in the layout cuFFT requires for input data. dstPointer and srcPointer must point to different cudaLibXtDesc structures (and therefore memory locations). That is, the copy cannot be in-place.

```
typedef enum cufftXtCopyType_t {
    CUFFT_COPY_HOST_TO_DEVICE,
    CUFFT_COPY_DEVICE_TO_HOST,
    CUFFT_COPY_DEVICE_TO_DEVICE
} cufftXtCopyType;
```

3.10.5. General Multiple GPU Descriptor Types

3.10.5.1. cudaXtDesc

A descriptor type used in multiple GPU routines that contains information about the GPUs and their memory locations.

```
struct cudaXtDesc_t{
  int version;
  int nGPUs;
  int GPUs[MAX_CUDA_DESCRIPTOR_GPUS];
  void *data[MAX_CUDA_DESCRIPTOR_GPUS];
  per GPU
    size_t size[MAX_CUDA_DESCRIPTOR_GPUS];
  void *cudaXtState;
};
typedef struct cudaXtDesc_t cudaXtDesc;
//descriptor version
//number of GPUs
//array of device IDs
//array of pointers to data, one
//array of data sizes, one per GPU
//opaque CUDA utility structure
```

3.10.5.2. cudaLibXtDesc

A descriptor type used in multiple GPU routines that contains information about the library used.

3.11. cuFFT Callbacks

3.11.1. Function cufftXtSetCallback()

```
cufftResult
   cufftXtSetCallback(cufftHandle plan, void **callbackRoutine,
   cufftXtCallbackType type, void **callerInfo)
```

cufftXtSetCallback() specifies a load or store callback to be used with the
plan. This call is valid only after a call to cufftMakePlan*(), which does the plan
generation. If there was already a callback of this type associated with the plan, this new
callback routine replaces it. If the new callback requires shared memory, you must call
cufftXtSetCallbackSharedSize with the amount of shared memory it needs. cuFFT
will not retain the amount of shared memory associated with the previous callback.

Input

plan	cufftHandle returned by cufftCreate
callbackRoutine	Array of callback routine pointers, one per GPU
type	type of callback routine
callerInfo	optional array of device pointers to caller specific information, one per GPU

CUFFT_SUCCESS	cuFFT successfully associated the callback function with the plan.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle, or a non-default stream has been associated with the plan.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.

3.11.2. Function cufftXtClearCallback()

cufftResult
 cufftXtClearCallback(cufftHandle plan, cufftXtCallbackType type)

cufftXtClearCallback() instructs cuFFT to stop invoking the specified callback type when executing the plan. Only the specified callback is cleared. If no callback of this type had been specified, the return code is **CUFFT_SUCCESS**.

Input

plan	cufftHandle returned by cufftCreate
type	type of callback routine

Return Values

CUFFT_SUCCESS	cuFFT successfully disassociated the callback function with the plan.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle, or a non-default stream has been associated with the plan.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.

3.11.3. Function cufftXtSetCallbackSharedSize()

cufftResult
 cufftXtSetCallbackSharedSize(cufftHandle plan, cufftXtCallbackType type,
 size_t sharedSize)

cufftXtSetCallbackSharedSize() instructs cuFFT to dynamically allocate shared memory at launch time, for use by the callback. The maximum allowable amount of shared memory is 16K bytes. cuFFT passes a pointer to this shared memory to the callback routine at execution time. This shared memory is only valid for the life of the load or store callback operation. During execution, cuFFT may overwrite shared memory for its own purposes.

Input

plan	cufftHandle returned by cufftCreate
type	type of callback routine
sharedSize	amount of shared memory requested

CUFFT_SUCCESS	cuFFT will invoke the callback routine with a pointer to the requested amount of shared memory.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle, or a non-default stream has been associated with the plan.
CUFFT_INTERNAL_ERROR	An internal driver error was detected.
CUFFT_ALLOC_FAILED	cuFFT will not be able to allocate the requested amount of shared memory.

3.12. Function cufftSetStream()

```
cufftResult
  cufftSetStream(cufftHandle plan, cudaStream t stream);
```

Associates a CUDA stream with a cuFFT plan. All kernel launches made during plan execution are now done through the associated stream, enabling overlap with activity in other streams (e.g. data copying). The association remains until the plan is destroyed or the stream is changed with another call to <code>cufftSetStream()</code>. This call will return an error for multiple GPU plans.

Input

plan	The cufftHandle object to associate with the stream
	A valid CUDA stream created with cudaStreamCreate(); 0 for the default stream

Status Returned

CUFFT_SUCCESS	The stream was associated with the plan.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle, or it is a multiple GPU plan.

3.13. Function cufftGetVersion()

```
cufftResult
  cufftGetVersion(int *version);
```

Returns the version number of cuFFT.

Input

version	Pointer to the version number

Output

version	Contains the version number
---------	-----------------------------

Return Values

CUFFT_SUCCESS	cuFFT successfully returned the version number.
---------------	---

3.14. Function cufftSetCompatibilityMode()

```
cufftResult
    cufftSetCompatibilityMode(cufftHandle plan, cufftCompatibility mode);
```

Configures the layout of cuFFT output in FFTW-compatible modes. When desired, FFTW compatibility can be configured for padding only, for asymmetric complex inputs

only, or for full compatibility. If the **cufftSetCompatibilityMode()** API fails, later **cufftExecute*()** calls are not guaranteed to work.

Input

plan	The cufftHandle object to associate with the stream
mode	The cufftCompatibility option to be used:
	CUFFT_COMPATIBILITY_NATIVE (deprecated) CUFFT_COMPATIBILITY_FFTW_PADDING (default) CUFFT_COMPATIBILITY_FFTW_ASYMMETRIC (deprecated) CUFFT_COMPATIBILITY_FFTW_ALL

Return Values

CUFFT_SUCCESS	cuFFT successfully set compatibiltiy mode.
CUFFT_INVALID_PLAN	The plan parameter is not a valid handle.
CUFFT_SETUP_FAILED	The cuFFT library failed to initialize.

3.15. Parameter cufftCompatibility

cuFFT Library defines FFTW compatible data layouts using the following enumeration of values. See FFTW Compatibility Mode for more details.

3.16. cuFFT Types

3.16.1. Parameter cufftType

The cuFFT library supports complex- and real-data transforms. The **cufftType** data type is an enumeration of the types of transform data supported by cuFFT.

3.16.2. Parameters for Transform Direction

The cuFFT library defines forward and inverse Fast Fourier Transforms according to the sign of the complex exponential term.

```
#define cuFFTFORWARD -1
#define cuFFTINVERSE 1
```

cuFFT performs un-normalized FFTs; that is, performing a forward FFT on an input data set followed by an inverse FFT on the resulting set yields data that is equal to the input, scaled by the number of elements. Scaling either transform by the reciprocal of the size of the data set is left for the user to perform as seen fit.

3.16.3. Type definitions for callbacks

The cuFFT library supports callback funtions for all combinations of single or double precision, real or complex data, load or store. These are enumerated in the parameter cufftXtCallbackType.

```
typedef enum cufftXtCallbackType_t {
    CUFFT_CB_LD_COMPLEX = 0x0,
    CUFFT_CB_LD_COMPLEX_DOUBLE = 0x1,
    CUFFT_CB_LD_REAL = 0x2,
    CUFFT_CB_LD_REAL_DOUBLE = 0x3,
    CUFFT_CB_ST_COMPLEX = 0x4,
    CUFFT_CB_ST_COMPLEX_DOUBLE = 0x5,
    CUFFT_CB_ST_REAL = 0x6,
    CUFFT_CB_ST_REAL_DOUBLE = 0x7,
    CUFFT_CB_UNDEFINED = 0x8
} cufftXtCallbackType;
```

The corresponding function prototypes and pointer type definitions are as follows:

```
typedef cufftComplex (*cufftCallbackLoadC)(void *dataIn, size t offset, void
 *callerInfo, void *sharedPointer);
typedef cufftDoubleComplex (*cufftCallbackLoadZ)(void *dataIn, size t offset,
void *callerInfo, void *sharedPointer);
typedef cufftReal (*cufftCallbackLoadR)(void *dataIn, size t offset, void
*callerInfo, void *sharedPointer);
typedef cufftDoubleReal(*cufftCallbackLoadD)(void *dataIn, size t offset, void
 *callerInfo, void *sharedPointer);
typedef void (*cufftCallbackStoreC)(void *dataOut, size t offset, cufftComplex
element, void *callerInfo, void *sharedPointer);
typedef void (*cufftCallbackStoreZ)(void *dataOut, size t offset,
cufftDoubleComplex element, void *callerInfo, void *sharedPointer);
typedef void (*cufftCallbackStoreR) (void *dataOut, size t offset, cufftReal
element, void *callerInfo, void *sharedPointer);
typedef void (*cufftCallbackStoreD) (void *dataOut, size t offset,
cufftDoubleReal element, void *callerInfo, void *sharedPointer);
```

3.16.4. Other cuFFT Types

3.16.4.1. cufftHandle

A handle type used to store and access cuFFT plans. The user receives a handle after creating a cuFFT plan and uses this handle to execute the plan.

typedef unsigned int cufftHandle;

3.16.4.2. cufftReal

A single-precision, floating-point real data type.

typedef float cufftReal;

3.16.4.3. cufftDoubleReal

A double-precision, floating-point real data type.

typedef double cufftDoubleReal;

3.16.4.4. cufftComplex

A single-precision, floating-point complex data type that consists of interleaved real and imaginary components.

typedef cuComplex cufftComplex;

3.16.4.5. cufftDoubleComplex

A double-precision, floating-point complex data type that consists of interleaved real and imaginary components.

typedef cuDoubleComplex cufftDoubleComplex;

Chapter 4. CUFFT CODE EXAMPLES

This chapter provides multiple simple examples of complex and real 1D, 2D, and 3D transforms that use cuFFT to perform forward and inverse FFTs.

4.1. 1D Complex-to-Complex Transforms

In this example a one-dimensional complex-to-complex transform is applied to the input data. Afterwards an inverse transform is performed on the computed frequency domain representation.

```
#define NX 256
#define BATCH 1
cufftHandle plan;
cufftComplex *data;
cudaMalloc((void**)&data, sizeof(cufftComplex)*NX*BATCH);
if (cudaGetLastError() != cudaSuccess) {
fprintf(stderr, "Cuda error: Failed to allocate\n");
return;
if (cufftPlan1d(&plan, NX, CUFFT C2C, BATCH) != CUFFT SUCCESS) {
fprintf(stderr, "CUFFT error: Plan creation failed");
return;
. . .
/* Note:
* Identical pointers to input and output arrays implies in-place
transformation
if (cufftExecC2C(plan, data, data, CUFFT_FORWARD) != CUFFT_SUCCESS) {
fprintf(stderr, "CUFFT error: ExecC2C Forward failed");
return;
if (cufftExecC2C(plan, data, data, CUFFT_INVERSE) != CUFFT_SUCCESS) {
fprintf(stderr, "CUFFT error: ExecC2C Inverse failed");
return:
* Results may not be immediately available so block device until all
   tasks have completed
if (cudaDeviceSynchronize() != cudaSuccess) {
fprintf(stderr, "Cuda error: Failed to synchronize\n");
return;
* Divide by number of elements in data set to get back original data
cufftDestroy(plan);
cudaFree (data);
```

4.2. 1D Real-to-Complex Transforms

In this example a one-dimensional real-to-complex transform is applied to the input data.

```
#define NX 256
#define BATCH 1
cufftHandle plan;
cufftComplex *data;
cudaMalloc((void**)&data, sizeof(cufftComplex)*(NX/2+1)*BATCH);
if (cudaGetLastError() != cudaSuccess){
fprintf(stderr, "Cuda error: Failed to allocate\n");
if (cufftPlan1d(&plan, NX, CUFFT R2C, BATCH) != CUFFT SUCCESS) {
fprintf(stderr, "CUFFT error: Plan creation failed");
. . .
/* Use the CUFFT plan to transform the signal in place. */
if (cufftExecR2C(plan, (cufftReal*)data, data) != CUFFT SUCCESS) {
fprintf(stderr, "CUFFT error: ExecC2C Forward failed");
return;
if (cudaDeviceSynchronize() != cudaSuccess) {
fprintf(stderr, "Cuda error: Failed to synchronize\n");
return;
. . .
cufftDestroy(plan);
cudaFree(data);
```

4.3. 2D Complex-to-Real Transforms

In this example a two-dimensional complex-to-real transform is applied to the input data arranged according to the requirements of the default FFTW padding mode.

```
#define NX 256
#define NY 128
#define NRANK 2
#define BATCH 1
cufftHandle plan;
cufftComplex *data;
int n[NRANK] = {NX, NY};
cudaMalloc((void**)&data, sizeof(cufftComplex)*NX*(NY/2+1));
if (cudaGetLastError() != cudaSuccess) {
fprintf(stderr, "Cuda error: Failed to allocate\n");
return;
/* Create a 2D FFT plan. */
if (cufftPlanMany(&plan, NRANK, n,
     NULL, 1, 0,
     NULL, 1, 0,
     CUFFT C2R, BATCH) != CUFFT SUCCESS) {
fprintf(stderr, "CUFFT Error: Unable to create plan\n");
if (cufftExecC2R(plan, data, data) != CUFFT SUCCESS) {
fprintf(stderr, "CUFFT Error: Unable to execute plan\n");
return;
if (cudaDeviceSynchronize() != cudaSuccess) {
   fprintf(stderr, "Cuda error: Failed to synchronize\n");
   return;
cufftDestroy(plan);
cudaFree (data);
```

4.4. 3D Complex-to-Complex Transforms

In this example a three-dimensional complex-to-complex transform is applied to the input data.

```
#define NX 64
#define NY 128
#define NZ 128
#define BATCH 10
#define NRANK 3
cufftHandle plan;
cufftComplex *data;
int n[NRANK] = \{NX, NY, NZ\};
cudaMalloc((void**)&data, sizeof(cufftComplex)*NX*NY*NZ*BATCH);
if (cudaGetLastError() != cudaSuccess){
fprintf(stderr, "Cuda error: Failed to allocate\n");
 return;
/* Create a 3D FFT plan. */
if (cufftPlanMany(&plan, NRANK, n,
 NULL, 1, NX*NY*NZ, // *inembed, istride, idist
NULL, 1, NX*NY*NZ, // *onembed, ostride, odist
CUFFT_C2C, BATCH) != CUFFT_SUCCESS) {
fprintf(stderr, "CUFFT error: Plan creation failed");
 return;
^{\prime \star} Use the CUFFT plan to transform the signal in place. ^{\star \prime}
if (cufftExecC2C(plan, data, data, CUFFT_FORWARD) != CUFFT_SUCCESS) {
 fprintf(stderr, "CUFFT error: ExecC2C Forward failed");
return;
if (cudaDeviceSynchronize() != cudaSuccess) {
 fprintf(stderr, "Cuda error: Failed to synchronize\n");
return;
. . .
cufftDestroy(plan);
cudaFree (data);
```

4.5. 2D Advanced Data Layout Use

In this example a two-dimensional complex-to-complex transform is applied to the input data arranged according to the requirements the advanced layout.

```
#define NX 128
#define NY 256
#define BATCH 10
#define NRANK 2
/\!\!^* Advanced interface parameters, arbitrary strides */ #define ISTRIDE 2 \, // distance between successive input elements in innermost
dimension
#define OSTRIDE 1
                   // distance between successive output elements in innermost
dimension
#define IX (NX+2)
#define IY (NY+1)
#define OX (NX+3)
#define OY (NY+4)
#define IDIST (IX*IY*ISTRIDE+3) // distance between first element of two
consecutive signals in a batch of input data
#define ODIST (OX*OY*OSTRIDE+5) // distance between first element of two
consecutive signals in a batch of output data
cufftHandle plan;
cufftComplex *idata, *odata;
int isize = IDIST * BATCH;
int osize = ODIST * BATCH;
int n[NRANK] = {NX, NY};
int inembed[NRANK] = {IX, IY}; // pointer that indicates storage dimensions of
input data
int onembed[NRANK] = {OX, OY}; // pointer that indicates storage dimensions of
output data
cudaMalloc((void **)&idata, sizeof(cufftComplex)*isize);
cudaMalloc((void **)&odata, sizeof(cufftComplex)*osize);
if (cudaGetLastError() != cudaSuccess) {
fprintf(stderr, "Cuda error: Failed to allocate\n");
return;
/* Create a batched 2D plan */
if (cufftPlanMany(&plan, NRANK, n,
      inembed, ISTRIDE, IDIST,
      onembed, OSTRIDE, ODIST,
      CUFFT C2C, BATCH) != CUFFT SUCCESS) {
 fprintf(stderr, "CUFFT Error: Unable to create plan\n");
return;
/* Execute the transform out-of-place */
if (cufftExecC2C(plan, idata, odata, CUFFT FORWARD) != CUFFT SUCCESS){
fprintf(stderr, "CUFFT Error: Failed to execute plan\n");
return;
if (cudaDeviceSynchronize() != cudaSuccess) {
   fprintf(stderr, "Cuda error: Failed to synchronize\n");
   return;
cufftDestroy(plan);
cudaFree (idata);
cudaFree (odata);
```

4.6. 3D Complex-to-Complex Transforms using Two GPUs

In this example a three-dimensional complex-to-complex transform is applied to the input data using two GPUs.

```
// Demonstrate how to use CUFFT to perform 3-d FFTs using 2 GPUs
// cufftCreate() - Create an empty plan
   cufftHandle plan input; cufftResult result;
   result = cufftCreate(&plan input);
   if (result != CUFFT SUCCESS) { printf ("*Create failed\n"); return; }
// cufftXtSetGPUs() - Define which GPUs to use
   int nGPUs = 2, whichGPUs[2];
   whichGPUs[0] = 0; whichGPUs[1] = 1;
   result = cufftXtSetGPUs (plan input, nGPUs, whichGPUs);
   if (result != CUFFT_SUCCESS) { printf ("*XtSetGPUs failed\n"); return; }
// Initialize FFT input data
   size t worksize[2];
   cufftComplex *host data input, *host data output;
   int nx = 64, ny = \overline{128}, \overline{nz} = 32;
   int size_of_data = sizeof(cufftComplex) * nx * ny * nz;
host_data_input = malloc(size_of_data);
   if (host_data_input == NULL) { printf ("malloc failed\n"); return; }
   host data output = malloc(size of data);
   if (host_data_output == NULL) { printf ("malloc failed\n"); return; }
   initialize_3d_data (nx, ny, nz, host_data_input, host_data_output);
// cufftMakePlan3d() - Create the plan
   result = cufftMakePlan3d (plan input, nz, ny, nx, CUFFT C2C, worksize);
   if (result != CUFFT_SUCCESS) { printf ("*MakePlan* failed\n"); return; }
// cufftXtMalloc() - Malloc data on multiple GPUs
   cudaLibXtDesc *device_data_input;
   result = cufftXtMalloc (plan_input, &device_data_input,
        CUFFT_XT_FORMAT_INPLACE);
   if (result != CUFFT SUCCESS) { printf ("*XtMalloc failed\n"); return; }
// cufftXtMemcpy() - Copy data from host to multiple GPUs
   result = cufftXtMemcpy (plan_input, device_data_input,
   host_data_input, CUFFT_COPY_HOST_TO_DEVICE);
if (result != CUFFT_SUCCESS) { printf ("*XtMemcpy failed\n"); return; }
// cufftXtExecDescriptorC2C() - Execute FFT on multiple GPUs
   result = cufftXtExecDescriptorC2C (plan input, device_data_input,
        device data input, CUFFT FORWARD);
   if (result != CUFFT SUCCESS) { printf ("*XtExec* failed\n"); return; }
// cufftXtMemcpy() - Copy data from multiple GPUs to host
   result = cufftXtMemcpy (plan_input, host_data_output,
        device data input, CUFFT COPY DEVICE TO HOST);
   if (result != CUFFT SUCCESS) { printf ("*XtMemcpy failed\n"); return; }
// Print output and check results
   int output return = output 3d results (nx, ny, nz,
       host data input, host data output);
   if (output return != 0) { return; }
// cufftXtFree() - Free GPU memory
   result = cufftXtFree(device_data_input);
   if (result != CUFFT SUCCESS) { printf ("*XtFree failed\n"); return; }
// cufftDestroy() - Destroy FFT plan
   result = cufftDestroy(plan input);
   if (result != CUFFT_SUCCESS) { printf ("*Destroy failed: code\n"); return; }
    free(host data input); free(host data output);
```

4.7. 1D Complex-to-Complex Transforms using Two GPUs with Natural Order

In this example a one-dimensional complex-to-complex transform is applied to the input data using two GPUs. The output data is in natural order in GPU memory.

```
// Demonstrate how to use CUFFT to perform 1-d FFTs using 2 GPUs
// Output on the GPUs is in natural output
// Function return codes should be checked for errors in actual code
// cufftCreate() - Create an empty plan
   cufftHandle plan_input; cufftResult result;
   result = cufftCreate(&plan_input);
// cufftXtSetGPUs() - Define which GPUs to use
   int nGPUs = 2, whichGPUs[2];
   whichGPUs[0] = 0; whichGPUs[1] = 1;
   result = cufftXtSetGPUs (plan_input, nGPUs, whichGPUs);
// Initialize FFT input data
   size t worksize[2];
   cufftComplex *host data input, *host data output;
   int nx = 1024, batch = \overline{1}, rank = 1, \overline{n}[1];
   int inembed[1], istride, idist, onembed[1], ostride, odist;
n[0] = nx;
   int size of data = sizeof(cufftComplex) * nx * batch;
   host data input = malloc(size of data);
   host data output = malloc(size_of_data);
   // cufftMakePlanMany() - Create the plan
   result = cufftMakePlanMany (plan_input, rank, n, inembed, istride, idist,
       onembed, ostride, odist, CUFFT C2C, batch, worksize);
// cufftXtMalloc() - Malloc data on multiple GPUs
   cudaLibXtDesc *device data input, *device data output;
   result = cufftXtMalloc (plan_input, &device_data_input,
      CUFFT_XT_FORMAT_INPLACE);
   result = cufftXtMalloc (plan_input, &device_data_output,
       CUFFT XT FORMAT INPLACE);
// cufftXtMemcpy() - Copy data from host to multiple GPUs
   result = cufftXtMemcpy (plan_input, device_data_input,
       host data input, CUFFT COPY HOST TO DEVICE);
// cufftXtExecDescriptorC2C() - Execute FFT on multiple GPUs
   result = cufftXtExecDescriptorC2C (plan input, device data input,
       device data input, CUFFT FORWARD);
// cufftXtMemcpy() - Copy the data to natural order on GPUs
   result = cufftXtMemcpy (plan_input, device_data_output,
       device data input, CUFFT COPY DEVICE TO DEVICE);
// Print output and check results
   int output_return = output_1d_results (nx, batch,
       host data input, host data output);
// cufftXtFree() - Free GPU memory
   result = cufftXtFree(device data input);
   result = cufftXtFree(device data output);
// cufftDestroy() - Destroy FFT plan
   result = cufftDestroy(plan_input);
   free(host data input); free(host data output);
```

4.8. 1D Complex-to-Complex Convolution using Two GPUs

In this example a one-dimensional convolution is calculated using complex-to-complex transforms.

```
// Demonstrate how to use CUFFT to perform a convolution using 1-d FFTs and
// 2 GPUs. The forward FFTs use both GPUs, while the inverse FFT uses one.
// Function return codes should be checked for errors in actual code.
// cufftCreate() - Create an empty plan
   cufftResult result; cudaError_t cuda_status;
   cufftHandle plan_forward_2_gpus, plan_inverse_1_gpu;
result = cufftCreate(&plan_forward_2_gpus);
   result = cufftCreate(&plan inverse 1 gpu);
// cufftXtSetGPUs() - Define which GPUs to use
   int nGPUs = 2, whichGPUs[2];
whichGPUs[0] = 0; whichGPUs[1] = 1;
   result = cufftXtSetGPUs (plan forward 2 gpus, nGPUs, whichGPUs);
// Initialize FFT input data
   size t worksize[2];
    cufftComplex *host_data_input, *host_data_output;
   int nx = 1048576, \overline{b}atch = 2, rank = \overline{1}, n[\overline{1}];
   int inembed[1], istride, idist, onembed[1], ostride, odist;
   n[0] = nx;
   int size_of_one_set = sizeof(cufftComplex) * nx;
int size_of_data = size_of_one_set * batch;
   host data input = (cufftComplex*)malloc(size of data);
   host data output = (cufftComplex*)malloc(size of one set);
   // cufftMakePlanMany(), cufftPlan1d - Create the plans
   result = cufftMakePlanMany (plan forward 2 gpus, rank, n, inembed,
       istride, idist, onembed, ostride, odist, CUFFT C2C, batch, worksize);
   result = cufftPlan1d (&plan_inverse_1_gpu, nx, CUFFT_C2C, 1);
// cufftXtMalloc(), cudaMallocHost - Allocate data for GPUs
   cudaLibXtDesc *device data input; cufftComplex *GPUO data from GPU1;
    result = cufftXtMalloc (plan_forward_2_gpus, &device_data_input,
        CUFFT_XT_FORMAT_INPLACE);
    int device0 = device data input->descriptor->GPUs[0];
   cudaSetDevice(device0) ;
   cuda status = cudaMallocHost ((void**)&GPU0 data from GPU1,size of one set);
// cufftXtMemcpy() - Copy data from host to multiple GPUs
   result = cufftXtMemcpy (plan_forward_2_gpus, device_data_input,
    host_data_input, CUFFT_COPY_HOST_TO_DEVICE);
// cufftXtExecDescriptorC2C() - Execute forward FFTs on multiple GPUs
    result = cufftXtExecDescriptorC2C (plan forward 2 gpus, device data input,
        device data input, CUFFT FORWARD);
// cudaMemcpy result from GPU1 to GPU0
   cufftComplex *device data on GPU1;
   device_data_on_GPU1 = (cufftComplex*)
        (device_data_input->descriptor->data[1]);
    cuda_status = cudaMemcpy (GPU0_data_from_GPU1, device_data on GPU1,
        size of one set, cudaMemcpyDeviceToDevice);
  Continued on next page
```

```
// Demonstrate how to use CUFFT to perform a convolution using 1-d FFTs and
// 2 GPUs. The forward FFTs use both GPUs, while the inverse FFT uses one.
// Function return codes should be checked for errors in actual code.
// Part 2
// Multiply results and scale output
   cufftComplex *device_data_on_GPU0;
   device_data_on_GPU0 = (cufftComplex*)
        (device data input->descriptor->data[0]);
   cudaSetDevice(device0) ;
   ComplexPointwiseMulAndScale<<<32, 256>>>((cufftComplex*)device data on GPU0,
       (cufftComplex*) GPU0 data from GPU1, nx);
// cufftExecC2C() - Execute inverse FFT on one GPU
   result = cufftExecC2C (plan_inverse_1_gpu, GPU0_data_from_GPU1,
       GPU0 data from GPU1, CUFFT INVERSE);
// cudaMemcpy() - Copy results from GPU0 to host
   cuda status = cudaMemcpy(host data output, GPUO data from GPU1,
       size of one set, cudaMemcpyDeviceToHost);
// Print output and check results
   int output_return = output_ld_results (nx, batch,
       host data input, host data output);
// cufftDestroy() - Destroy FFT plans
   result = cufftDestroy(plan forward 2 gpus);
   result = cufftDestroy(plan_inverse_1_gpu);
// cufftXtFree(), cudaFreeHost(), free() - Free GPU and host memory
   result = cufftXtFree(device_data_input);
   cuda status = cudaFreeHost (GPU0 data from GPU1);
   free (host data input); free (host data output);
```

```
//
// Utility routine to perform complex pointwise multiplication with scaling
__global___ void ComplexPointwiseMulAndScale
        (cufftComplex *a, cufftComplex *b, int size)
{
        const int numThreads = blockDim.x * gridDim.x;
        const int threadID = blockIdx.x * blockDim.x + threadIdx.x;
        float scale = 1.0f / (float)size;
        cufftComplex c;
        for (int i = threadID; i < size; i += numThreads)
        {
            c = cuCmulf(a[i], b[i]);
            b[i] = make_cuFloatComplex(scale*cuCrealf(c), scale*cuCimagf(c));
        }
        return;
}</pre>
```

Chapter 5. MULTIPLE GPU DATA ORGANIZATION

This chapter explains how data are distributed between the GPUs, before and after a multiple GPU transform. For simplicity, it is assumed in this chapter that the caller has specified GPU 0 and GPU 1 to perform the transform.

5.1. Multiple GPU Data Organization for Batched Transforms

For batches of transforms, each individual transform is executed on a single GPU. If possible the batches are evenly distributed among the GPUs. For a batch of size \mathbf{m} performed on \mathbf{n} GPUs, where \mathbf{m} is not divisible by \mathbf{n} , the first \mathbf{m} % \mathbf{n} GPUs will perform $\left\lfloor \frac{\mathbf{m}}{\mathbf{n}} \right\rfloor + 1$ transforms. The remaining GPUs will perform $\left\lfloor \frac{\mathbf{m}}{\mathbf{n}} \right\rfloor$ transforms. For example, in a batch of 15 transforms performed on 4 GPUs, the first three GPUs would perform 4 transforms, and the last GPU would perform 3 transforms. This approach removes the need for data exchange between the GPUs, and results in nearly perfect scaling for cases where the batch size is divisible by the number of GPUs.

5.2. Multiple GPU Data Organization for Single 2D and 3D Transforms

Single transforms performed on multiple GPUs require the data to be divided between the GPUs. Then execution takes place in phases. For example with 2 GPUs, for 2D and 3D transforms with even sized dimensions, each GPU does half of the transform in (rank - 1) dimensions. Then data are exchanged between the GPUs so that the final dimension can be processed.

Since 2D and 3D transforms support sizes other than powers of 2, it is possible that the data can not be evenly distributed among the GPUs. In general for the case of **n** GPUs, a dimension of size **m** that is not a multiple of **n** would be distributed such that the first **m** % **n** GPUs would get one extra row for 2D transforms, one extra plane for 3D transforms.

Take for example, a 2D transform on 4 GPUs, using an array declared in C as data[x] [y], where x is 65 and y is 99. The surface is distributed prior to the transform such that GPU 0 receives a surface with dimensions [17][99], and GPUs 1...3 receive surfaces with dimensions [16][99]. After the transform, each GPU again has a portion of the surface, but divided in the y dimension. GPUs 0...2 have surfaces with dimensions [65] [25]. GPU 3 has a surface with dimensions [65] [24]

For a 3D transform on 4 GPUs consider an array declared in C as data[x][y][z], where x is 103, y is 122, and z is 64. The volume is distributed prior to the transform such that each GPUs 0...2 receive volumes with dimensions [26][122][64], and GPU 3 receives a volume with dimensions [26][101][64]. After the transform, each GPU again has a portion of the surface, but divided in the y dimension. GPUs 0 and 1 have a volumes with dimensions [103][31][64], and GPUs 2 and 3 have volumes with dimensions [103][30][64].

5.3. Multiple-GPU Data Organization for Single 1D Transforms

By default for 1D transforms, the initial distribution of data to the GPUs is similar to the 2D and 3D cases. For a transform of dimension x on two GPUs, GPU 0 receives data ranging from 0...(x/2-1). GPU 1 receives data ranging from (x/2)...(x-1). Similarly, with 4 GPUs, the data are evenly distributed among all 4 GPUs.

Before computation can begin, data are redistributed among the GPUs. It is possible to perform this redistribution in the copy from host memory, in cases where the application does not need to pre-process the data prior to the transform. To do this, the application can create the data descriptor with <code>cufftxtmalloc</code> using the sub-format <code>CUFFT_XT_FORMAT_1D_INPUT_SHUFFLED</code>. This can significantly reduce the time it takes to execute the transform.

cuFFT performs multiple GPU 1D transforms by decomposing the transform size into factors Factor1 and Factor2, and treating the data as a grid of size Factor1 x Factor2. The four steps done to calculate the 1D FFT are: Factor1 transforms of size Factor2, data exchange between the GPUs, a pointwise twiddle multiplication, and Factor2 transforms of size Factor1.

To gain efficiency by overlapping computation with data exchange, cuFFT breaks the whole transform into independent segments or strings, which can be processed while others are in flight. A side effect of this algorithm is that the output of the transform is not in linear order. The output in GPU memory is in strings, each of which is composed of Factor2 substrings of equal size. Each substring contains contiguous results starting Factor1 elements subsequent to start of the previous substring. Each string starts

substring size elements after the start of the previous string. The strings appear in order, the first half on GPU 0, and the second half on GPU 1. See the example below:

```
transform size = 1024
number of strings = 8
Factor1 = 64
Factor2 = 16
substrings per string for output layout is Factor2 (16)
string size = 1024/8 = 128
substring size = 128/16 = 8
stride between substrings = 1024/16 = Factor1 (64)

On GPU 0:
string 0 has substrings with indices 0...7 64...71 128...135 ... 960...967
string 1 has substrings with indices 8...15 72...79 136...143 ... 968...975
...
On GPU 1:
string 4 has substrings with indices 32...39 96...103 160...167 ... 992...999
...
string 7 has substrings with indices 56...63 120...127 184...191 ... 1016...1023
```

The cufftXtQueryPlan API allows the caller to retrieve a structure containing the number of strings, the decomposition factors, and (in the case of power of 2 size) some useful mask and shift elements. The example below shows how cufftXtQueryPlan is invoked. It

also shows how to translate from an index in the host input array to the corresponding index on the device, and vice versa.

```
* These routines demonstrate the use of cufftXtQueryPlan to get the 1D
^{\star} factorization and convert between permuted and linear indexes.
^{\star} Set up a 1D plan that will execute on GPU 0 and GPU1, and query
* the decomposition factors
int main(int argc, char **argv) {
   cufftHandle plan;
    cufftResult stat;
   int whichGPUs[2] = { 0, 1 };
   cufftXt1dFactors factors;
   stat = cufftCreate( &plan );
    if (stat != CUFFT_SUCCESS) {
        printf("Create error %d\n", stat);
        return 1;
    stat = cufftXtSetGPUs( plan, 2, whichGPUs );
   if (stat != CUFFT_SUCCESS) {
    printf("SetGPU error %d\n", stat);
        return 1;
    stat = cufftMakePlan1d( plan, size, CUFFT_C2C, 1, workSizes );
    if (stat != CUFFT_SUCCESS) {
        printf("MakePlan error %d\n", stat);
        return 1;
    stat = cufftXtQueryPlan( plan, (void *) &factors, CUFFT QUERY 1D FACTORS );
    if (stat != CUFFT_SUCCESS) {
       printf("QueryPlan error %d\n", stat);
        return 1;
    printf("Factor 1 %zd, Factor2 %zd\n", factors.factor1, factors.factor2);
    cufftDestroy(plan);
    return 0;
```

```
* Given an index into a permuted array, and the GPU index return the
* corresponding linear index from the beginning of the input buffer.
* Parameters:
                  input: pointer to cufftXtldFactors as returned by
       factors
                            cufftXtQueryPlan
       permutedIx input: index of the desired element in the device output
                            array
       linearIx output: index of the corresponding input element in the
                            host array
       GPUix
                   input: index of the GPU containing the desired element
cufftResult permuted2Linear( cufftXt1dFactors * factors,
                             size_t permutedIx,
                             size_t *linearIx,
int GPUIx ) {
   size t indexInSubstring;
   size t whichString;
   size t which Substring;
    // \overline{	heta} low order bits of the permuted index match those of the linear index
   indexInSubstring = permutedIx & factors->substringMask;
   // the next higher bits are the substring index
   whichSubstring = (permutedIx >> factors->substringShift) &
                     factors->factor2Mask;
    // the next higher bits are the string index on this GPU
   whichString = (permutedIx >> factors->stringShift) & factors->stringMask;
    // now adjust the index for the second GPU
   if (GPUIx) {
       whichString += factors->stringCount/2;
    // linear index low order bits are the same
    // next higher linear index bits are the string index
   *linearIx = indexInSubstring + ( whichString << factors->substringShift );
    // next higher bits of linear address are the substring index
   *linearIx += whichSubstring << factors->factor1Shift;
   return CUFFT SUCCESS;
```

```
* Given a linear index into a 1D array, return the GPU containing the permuted
* result, and index from the start of the data buffer for that element.
 * Parameters:
       factors
                    input: pointer to cufftXt1dFactors as returned by
                            cufftXtQueryPlan
       linearIx
                    input: index of the desired element in the host input
                            array
       permutedIx output: index of the corresponding result in the device
                            output array
       GPUix
                    output: index of the GPU containing the result
cufftResult linear2Permuted( cufftXt1dFactors * factors,
                             size_t linearIx,
                             size_t *permutedIx,
int *GPUIx ) {
   size t indexInSubstring;
   size t whichString;
   size t which Substring;
   size t whichStringMask;
   int whichStringShift;
   if (linearIx >= factors->size) {
       return CUFFT INVALID VALUE;
    // get a useful additional mask and shift count
   whichStringMask = factors->stringCount -1;
   whichStringShift = (factors->factor1Shift + factors->factor2Shift) -
                        factors->stringShift;
    // the low order bits identify the index within the substring
   indexInSubstring = linearIx & factors->substringMask;
    // first determine which string has our linear index.
    // the low order bits indentify the index within the substring.
   // the next higher order bits identify which string.
   whichString = (linearIx >> factors->substringShift) & whichStringMask;
    // the first stringCount/2 strings are in the first GPU,
    // the rest are in the second.
   *GPUIx = whichString/(factors->stringCount/2);
    // next determine which substring within the string has our index
    // the substring index is in the next higher order bits of the index
   whichSubstring = (linearIx >>(factors->substringShift + whichStringShift)) &
                      factors->factor2Mask;
    // now we can re-assemble the index
    *permutedIx = indexInSubstring;
    *permutedIx += whichSubstring << factors->substringShift;
   if ( !*GPUIx ) {
        *permutedIx += whichString << factors->stringShift;
    } else {
        *permutedIx += (whichString - (factors->stringCount/2) ) <<
                       factors->stringShift;
   return CUFFT SUCCESS;
```

Chapter 6. FFTW CONVERSION GUIDE

cuFFT differs from FFTW in that FFTW has many plans and a single execute function while cuFFT has fewer plans, but multiple execute functions. The cuFFT execute functions determine the precision (single or double) and whether the input is complex or real valued. The following table shows the relationship between the two interfaces.

FFTW function	cuFFT function
<pre>fftw_plan_dft_1d(), fftw_plan_dft_r2c_1d(), fftw_plan_dft_c2r_1d()</pre>	cufftPlan1d()
<pre>fftw_plan_dft_2d(), fftw_plan_dft_r2c_2d(), fftw_plan_dft_c2r_2d()</pre>	cufftPlan2d()
<pre>fftw_plan_dft_3d(), fftw_plan_dft_r2c_3d(), fftw_plan_dft_c2r_3d()</pre>	cufftPlan3d()
<pre>fftw_plan_dft(), fftw_plan_dft_r2c(), fftw_plan_dft_c2r()</pre>	cufftPlanMany()
<pre>fftw_plan_many_dft(), fftw_plan_many_dft_r2c(), fftw_plan_many_dft_c2r()</pre>	cufftPlanMany()
fftw_execute()	<pre>cufftExecC2C(), cufftExecZ2Z(), cufftExecR2C(), cufftExecD2Z(), cufftExecC2R(), cufftExecZ2D()</pre>
fftw_destroy_plan()	cufftDestroy()

Chapter 7. FFTW INTERFACE TO CUFFT

NVIDIA provides FFTW3 interfaces to the cuFFT library. This allows applications using FFTW to use NVIDIA GPUs with minimal modifications to program source code. To use the interface first do the following two steps

- ▶ It is recommended that you replace the include file fftw3.h with cufftw.h
- Instead of linking with the double/single precision libraries such as fftw3/fftw3f libraries, link with both the cuFFT and cuFFTW libraries
- Ensure the search path includes the directory containing cuda_runtime_api.h

After an application is working using the FFTW3 interface, users may want to modify their code to move data to and from the GPU and use the routines documented in the FFTW Conversion Guide for the best performance.

The following tables show which components and functions of FFTW3 are supported in cuFFT.

Section in FFTW manual	Supported	Unsupported
Complex numbers	<pre>fftw_complex, fftwf_complex types</pre>	
Precision	double fftw3, single fftwf3	long double fftw31, quad precision fftw3q are not supported since CUDA functions operate on double and single precision floating-point quantities
Memory Allocation		<pre>fftw_malloc(), fftw_free(), fftw_alloc_real(), fftw_alloc_complex(), fftwf_alloc_real(), fftwf_alloc_complex()</pre>
Multi-threaded FFTW		fftw3_threads, fftw3_omp are not supported
Distributed-memory FFTW with MPI		<pre>fftw3_mpi,fftw3f_mpi are not supported</pre>

Note that for each of the double precision functions below there is a corresponding single precision version with the letters fftw replaced by fftwf.

Section in FFTW manual	Supported	Unsupported
Using Plans	<pre>fftw_execute(), fftw_destroy_plan(), fftw_cleanup(), fftw_print_plan()</pre>	<pre>fftw_cost(), fftw_flops() exist but are not functional</pre>
Basic Interface		
Complex DFTs	<pre>fftw_plan_dft_1d(), fftw_plan_dft_2d(), fftw_plan_dft_3d(), fftw_plan_dft()</pre>	
Planner Flags		Planner flags are ignored and the same plan is returned regardless
Real-data DFTs	<pre>fftw_plan_dft_r2c_ld(), fftw_plan_dft_r2c_2d(), fftw_plan_dft_r2c_3d(), fftw_plan_dft_r2c(), fftw_plan_dft_c2r_ld(), fftw_plan_dft_c2r_2d(), fftw_plan_dft_c2r_3d(), fftw_plan_dft_c2r()</pre>	
Read-data DFT Array Format		Not supported
Read-to-Real Transform		Not supported
Read-to-Real Transform Kinds		Not supported
Advanced Interface		
Advanced Complex DFTs	fftw_plan_many_dft() with multiple 1D, 2D, 3D transforms	fftw_plan_many_dft() with 4D or higher transforms or a 2D or higher batch of embedded transforms
Advanced Real-data DFTs	fftw_plan_many_dft_r2c(), fftw_plan_many_dft_c2r() with multiple 1D, 2D, 3D transforms	fftw_plan_many_dft_r2c(), fftw_plan_many_dft_c2r() with 4D or higher transforms or a 2D or higher batch of embedded transforms
Advanced Real-to-Real Transforms		Not supported
Guru Interface		
Interleaved and split arrays	Interleaved format	Split format
Guru vector and transform sizes	fftw_iodim struct	
Guru Complex DFTs	<pre>fftw_plan_guru_dft(), fftw_plan_guru_dft_r2c(), fftw_plan_guru_dft_c2r() With multiple 1D, 2D, 3D transforms</pre>	<pre>fftw_plan_guru_dft(), fftw_plan_guru_dft_r2c(), fftw_plan_guru_dft_c2r() With</pre>

Section in FFTW manual	Supported	Unsupported
		4D or higher transforms or a 2D or higher batch of transforms
Guru Real-data DFTs		Not supported
Guru Real-to-real Transforms		Not supported
64-bit Guru Interface		Not supported
New-array Execute Functions	<pre>fftw_execute_dft(), fftw_execute_dft_r2c(), fftw_execute_dft_c2r() with interleaved format</pre>	Split format and real-to-real functions
Wisdom		<pre>fftw_export_wisdom_to_file(), fftw_import_wisdom_from_file() exist but are not functional. Other wisdom functions do not have entry points in the library.</pre>

Chapter 8. DEPRECATED FUNCTIONALITY

The cuFFT native data layout, specified by **CUFFT_COMPATIBILITY_NATIVE** has been deprecated. Use **CUFFT_COMPATIBILITY_FFTW_PADDING**.

The cufft asymmetric data input layout, specified by CUFFT_COMPATIBILITY_FFTW_ASYMMETRIC has been deprecated. Use CUFFT_COMPATIBILITY_FFTW_PADDING. cufft always treats asymmetric input in the same way as FFTW.

Batch sizes other than 1 for **cufftPlan1d()** have been deprecated. Use **cufftPlanMany()** for multiple batch execution.

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