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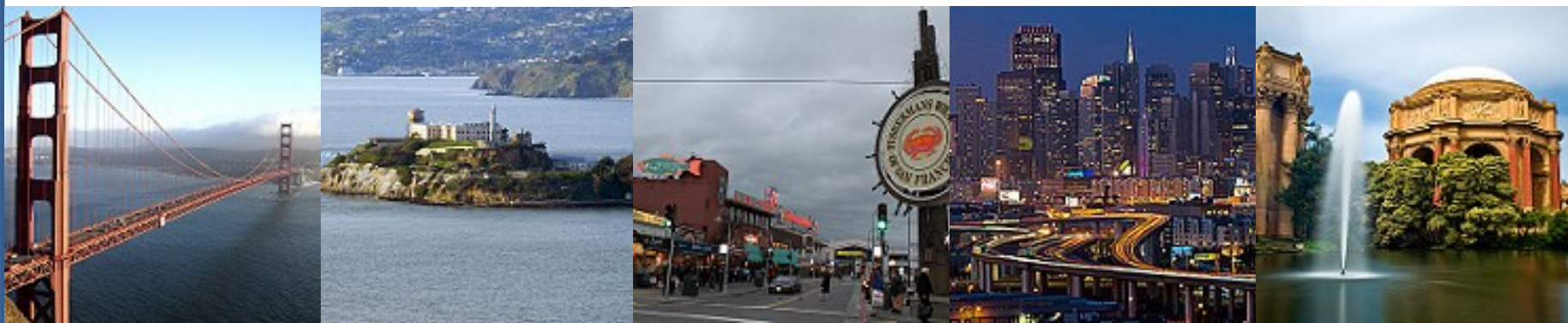
An efficient map-reduce algorithm for spatio-temporal analysis using Spark (GIS Cup)

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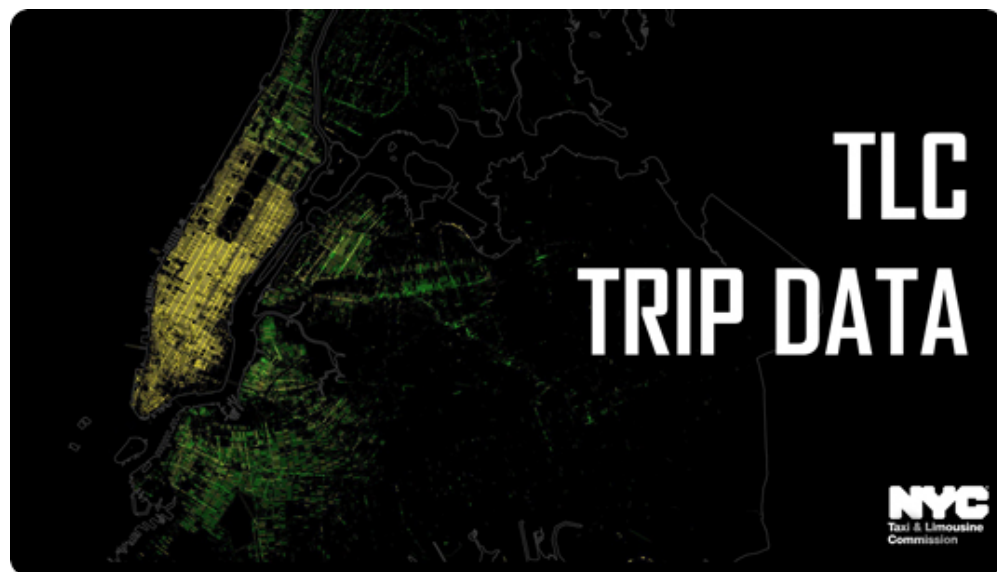
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NYC taxi trip dataset

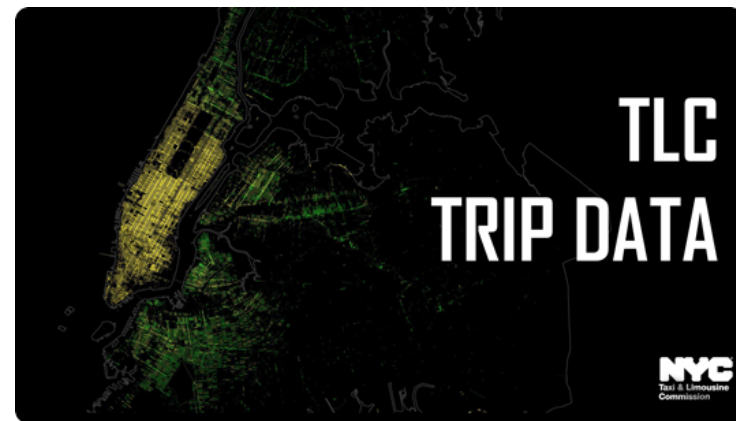
- NYC Taxi and Limousine Commission (TLC)
- > 1 billion records
- Since 2009
- Several CSV files containing:
 - Drop-off lat/long/time
 - Pick-up lat/long/time
 - Number of passengers
 - Trip distance
 - Fare
 - Payment type
 - Tolls
 - Etc.



Source: <http://www.nyc.gov>

NYC taxi trip dataset

- Big amount of information → many possibilities of analysis
- Example:
 - What is the average price of trips from JFK to LGA?
 - Is the most used type of payment different for different neighborhoods/days/hours?
 - What is the most frequent destination from Penn Station?
 - Hotspots for full taxis?
- Some interesting observations (2015 dataset).
 - Most frequent fare: \$7.80 (3,804,101
 - 195 trips cost more than \$1,000 (noise?)
 - # trips costing $(0, \$1]$: 35,893
 - Average # of passengers per trip: 1.6



Source: <http://www.nyc.gov>

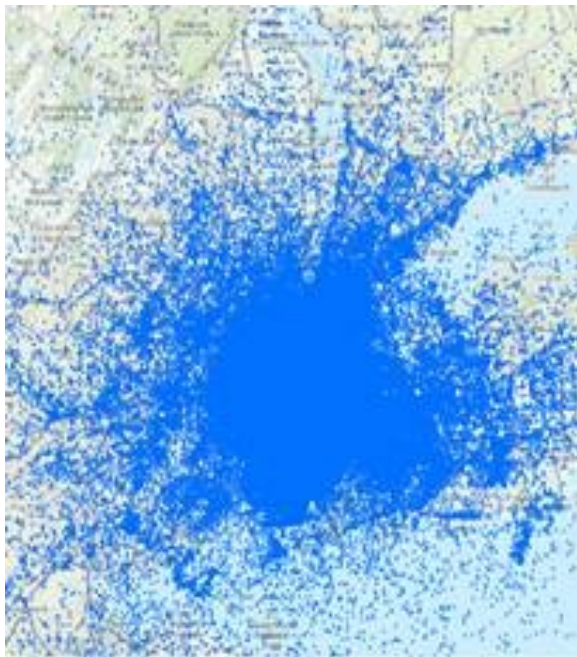
NYC taxi trip dataset

- Has some errors.

Pickup time	Drop-off time	Dist. (miles)	Pickup long.	Pickup lat.	Fare (USD)	Tip (USD)
03/29/2015 00:14:32	03/29/2015 00:28:41	1030	0.0000	0.0000	4800.21	0
09/20/2015 21:50:26	09/20/2015 21:52:57	1.2	0.0000	0.0000	8004.5	1200.8
11/25/2015 08:24:50	11/25/2015 08:51:53	7.5	-73.8705	40.7736	93977.3	0
12/27/2015 03:45:54	12/27/2015 03:45:54	0	-73.9289	40.7061	825998.61	0
01/18/2015 19:24:15	01/18/2015 19:51:55	5.3	-74.0021	40.7395	22	3950588.8

GISCUP 2016

- Given the 2015 dataset → what are the top 50 spatio-temporal hotspots?
- Consider the number of passengers being dropped-off.
- Clip the dataset to eliminate noise; consider only the 5 boroughs – remove dropoffs in the Atlantic Ocean.
- Filter drop-offs that happened in 2015. (e.g. remove New Years' Eve)



Source: GISCUP 2016

Hot-spot analysis

- Filtering bounding-box (5 boroughs, only 2015) → spatio-temporal cube.
- Aggregation: cell $i \rightarrow$ compute c_i (# passengers dropped-off)
- We can optionally always assume that $c_i = 1$.
- Compute the Getis-Ord G_i^* statistic.
- It's a z-score measure of statistical significance.

$$G_i^* = \frac{\sum_{j=1}^n w_{i,j} c_j - \bar{c} \sum_{j=1}^n w_{i,j}}{S \sqrt{\frac{n \sum_{j=1}^n w_{i,j}^2 - (\sum_{j=1}^n w_{i,j})^2}{n-1}}}$$

$$\bar{c} = \frac{\sum_{i=1}^n c_i}{n}$$

$$S = \sqrt{\frac{\sum_{i=1}^n c_i^2}{n} - \bar{c}^2}$$

Map-reduce history

- **Map-reduce: Functional Programming (FP)** concept.
- FP applies nested functions to sets of data..
- **Reduction:** component of high level languages at least since the APL language, proposed in 1957, operated on vectors and arrays.
- Implemented by IBM in 1965, widely used for some years.
- Thinking Machines CM-2 (Connection Machine 2) implemented hardware reduction in 1990.
- Google adopted map-reduce in 2004.
- Map-reduce is implemented well in parallel libraries like OpenMP and CUDA/Thrust.

Parallelism

- Serial processors have scarcely gotten faster in 5 years.
- It's a physics problem; must go parallel.
- Or use more efficient algorithms, or make a fundamental discovery.
- Communication dominates computation: keep the data close.
- 1st choice: large amounts of memory (*2TB workstations exist*).
- Plus multicore Intel Xeon CPUs. (*I have a dual 14-core machine*).
- 2nd choice: Nvidia GPUs
 - 1000s of slow CUDA cores. (20 CUDA cores = 1 Xeon core).. - Very complicated programming.
- 3rd choice: more distributed systems.

Hot-spot analysis

- $w_{i,j}$: 1 for neighbor cells, 0 for other pairs
- Interior cells: 26+1 neighbors; border cells: 8, 12, or 18.
- Let ν_i be the number of neighbors of i .
- We can optionally always use $\nu_i = 27$.
- Let **the sum of neighbors** be

$$\sigma_i = \sum_{j=1}^n w_{i,j} c_j$$

- Computing that is by far the hardest step.
- Then

$$G_i^* = \frac{\sigma_i - \bar{c}\nu_i}{S \sqrt{\frac{n\nu_i - \nu_i^2}{n-1}}}$$

Computing the “sum of neighbors”



“cell” coordinates

- Simple map-reduce algorithm
 - First step:
 1. Read files from HDFS and create a pair RDD: $((t, x, y), \text{drop_off})$
 2. Reduce by key
 3. Now: $\{((t, x, y), c)\}$
 4. Compute statistics
 - Second step (sum of neighbors):
 1. Each cell $((t, x, y), c) \rightarrow \{((t + d_t, x + d_x, y + d_y), c), d_t, d_x, d_y = -1..1\}$
 2. Reduce by key
 3. Now: $\{((t, x, y), \sigma)\}$
 - Third step:
 1. Compute G_i^* using σ /statistics
 2. Get top cells
- Implemented in Java+Spark

Optimizing the coordinate representation

Optimization:

- Java `Tuple3<Integer,Integer,Integer>` (generic class) internally uses three pointers to reference the integers.
- Big overhead for a class that simply stores three integers.
- Customized classes avoid pointers.
- Therefore we create a custom class with 3 integers

Optimizing the coordinate representation

Optimization:

- Represent “small coordinate tuple” as a single integer.
 - $(t,x,y) \rightarrow t \times (1+\text{MAX}_y) \times (1+\text{MAX}_x) + y \times (1+\text{MAX}_x) + x$
 - Easily handles 2G cells (4G would be possible).
 - *Note that ARCGIS space-time cubes have same limitation.*
 - Saves memory and I/O.
 - Faster comparison/hashing.
 - We also implement the general and slow data structure in case the user wants over 2G cells.

Computing the “sum of neighbors”

- Reading and parsing is the slowest step.
 - Use a custom parser (up to 2x speedup)
 - Recommendation: store the data in binary, not CSV.
- Spark configuration:
 - Kryo serializer
 - Convert between internal Java object and byte stream for file.
 - Many systems use it.
 - It trades security for speed, but that’s ok here.
 - Hash shuffler
 - To get the data from the mapper to the reducer.
 - Various shufflers are available.

Computing the “sum of neighbors”

- Most important optimization:
 - create an RDD with 27 times # of cells
 - Each cell $((t, x, y), c) \rightarrow \{((t+d_t, x+d_x, y+d_y), c), d_t, d_x, d_y = -1..1\}$
 - Before: element type stored in the RDD is a cell
 - Now: each element is a partition of the space-time cube.

3	2	7	8	1	7
2	1	3	9	9	3
4	5	4	1	1	0
9	3	8	7	2	1
1	2	4	2	7	7
2	4	2	1	9	4

• From:
 $(0,0),2;(1,0),4;(2,0),2;(3,0),1;(4,0),9;(5,0),4;(1,0),1; \dots$

• To:

$(0,0),$	<table><tr><td>9</td><td>3</td><td>8</td></tr><tr><td>1</td><td>2</td><td>4</td></tr><tr><td>2</td><td>4</td><td>2</td></tr></table>	9	3	8	1	2	4	2	4	2	$;(1,0),$	<table><tr><td>7</td><td>2</td><td>1</td></tr><tr><td>2</td><td>7</td><td>7</td></tr><tr><td>1</td><td>9</td><td>4</td></tr></table>	7	2	1	2	7	7	1	9	4	$;(0,1),$	<table><tr><td>3</td><td>2</td><td>7</td></tr><tr><td>2</td><td>1</td><td>3</td></tr><tr><td>4</td><td>5</td><td>4</td></tr></table>	3	2	7	2	1	3	4	5	4	$;(1,1),$	<table><tr><td>8</td><td>1</td><td>7</td></tr><tr><td>9</td><td>9</td><td>3</td></tr><tr><td>1</td><td>1</td><td>0</td></tr></table>	8	1	7	9	9	3	1	1	0
9	3	8																																									
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1	1	0																																									

Computing the “sum of neighbors”

- Improved solution:
 - More locality:
 - Sum of neighbors: *for* loop to add elements
 - Cells in boundary: special case (separate list and aggregate)
 - Fewer (but larger) elements:
 - Less overhead (implicit coordinates)

3	2	7	8	1	7
2	1	3	9	9	3
4	5	4	1	1	0
9	3	8	7	2	1
1	2	4	2	7	7
2	4	2	1	9	4

(0,0),2;(1,0),4;(2,0),2;(3,0),1;(4,0),9;(5,0),4;(1,0),1; ...

Failed idea: sample the data

Before settling on the previous algorithm, we tested several other ideas, but they were bad.

Failed idea: sample the data.

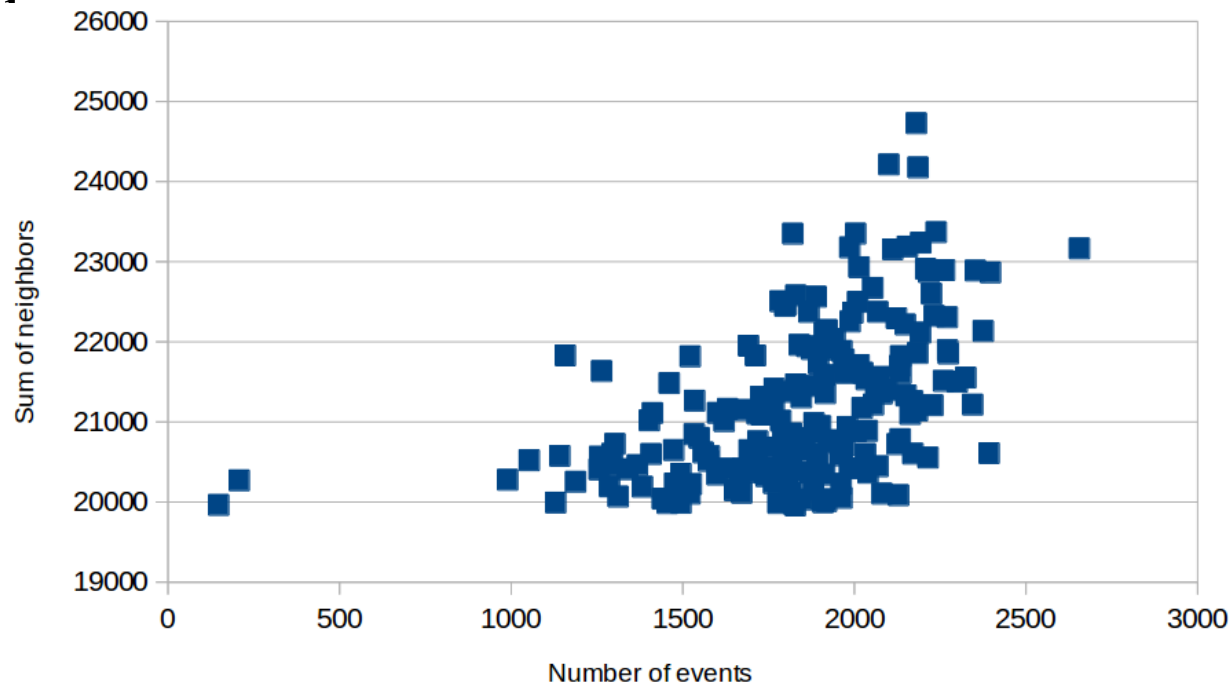
- Sampling large datasets is a common operation in statistics.
- Relative error falls with $\sqrt{\text{sample size}}$.
- So: Compute the hot spots for only some of the data.
- However: the list of hot spots changes.
- Fail.

Failed idea: allocate complete array of counts

- Failed idea: Instead of storing $((t,x,y), \text{count})$ tuples, allocate a complete array to store the counts.
- However most of the array would be 0.
- This would take more space (= more time).

Failed idea: count neighbors for only hot cells

- Perhaps a cell with high G_i^* will itself have many events.
- That is, regions of many events are several cells wide.
- So, count number of events for all cells.
- Pick the top 1000 cells.
- Count neighbors and compute G_i^* for only them.
- However, this doesn't always work.
- Some cells are like a donut hole.
- Plot: 2015 top 50, res: 0.001° , 1 day.



Experiments



- Amazon EC2
- 25x (1+24) m2.2xlarge
 - 4 CPUs
 - 34.2 GB of RAM
 - 850 GB rotational hard drive
- 2015 dataset (stored in HDFS)
- Algorithms/improvements:
 - Simple algorithm
 - K: Kryo serializer
 - H: Hash shuffler
 - C: Compressed coordinates
 - CP: Cube partitioning

Experiments

Spat. size	Time size	Algorithm			
		Simple	K+H	K+H+C	K+H+CP
0.01	30	18	20	19	21
0.01	7	18	20	19	19
0.01	1	26	20	20	19
0.001	30	20	20	19	25
0.001	7	27	23	22	22
0.001	1	37	27	24	24
0.0003	30	39	27	22	28
0.0003	7	65	42	25	25
0.0003	1	114	70	51	33
0.0001	30	84	61	30	25
0.0001	7	321	212	49	27
0.0001	1	675	455	-	33
0.00005	30	229	147	45	28
0.00005	7	1102	712	-	31
0.00005	1	1921	1318	-	37

Experiments

- $0.0001^\circ \rightarrow \sim 8\text{m} \times 11\text{m}$
 - 0.0001° , 1 day \rightarrow Bounding-box with: $4000 \times 5500 \times 365$ - 8G cells!
 - ~ 146 million trips in 2015
 - ~ 144 million filtered events (bounding-box)
 - $\rightarrow 0.02$ trips per cell, 0.03 drop-offs/cell
 - Hotspots:
 - long, lat, days from 1/1/2015, z-score, sum_neighbors
 - -73.9913,40.7501,352,1427.6,4207
 - -73.9913,40.7501,353,1413.1,4164
 - -73.9912,40.7502,114,1324.5,3903
 - -74.0001,40.7585,11,1323.1,3899
 - -73.9913,40.7501,114,1314.3,3873
 - -74.0000,40.7586,11,1311.9,3866
 - -73.9913,40.7502,352,1307.2,3852
 - -73.9912,40.7502,93,1306.8,3851
 - -73.9912,40.7502,353,1305.8,3848
 - -73.9913,40.7501,354,1303.8,3842

Conclusions

- Spark Map-Reduce:
 - Simple to implement
 - Can achieve good performance
- Best optimizations:
 - Compact coordinates
 - Cube partitioning

Up to 52x faster than simplest algorithm

Thank you!

$$G_i^* = \frac{\sigma_i - \bar{c}\nu_i}{S\sqrt{\frac{n\nu_i - \nu_i^2}{n-1}}}$$

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9	3	8	7	2	1
1	2	4	2	7	7
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0.001	7	27	23	22	22
0.001	1	37	27	24	24
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(0,0),2;(1,0),4;(2,0),2;(3,0),1;(4,0),9;(5,0),4;(1,0),1; ...

Acknowledgement:



(0,0),

9	3	8
1	2	4
2	4	2

 ;(1,0),

7	2	1
2	7	7
1	9	4

 ;(0,1),

3	2	7
2	1	3
4	5	4

 ;(1,1),

8	1	7
9	9	3
1	1	0

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