

C5 11/30/20-1

C = CHIP IS GOOD

$$P[C] = 1 - p = .9$$

$$P[\bar{C}] = p = 0.1$$

$$P[\text{ALIVE} @ t | \text{GOOD}] = e^{-\lambda t}$$

$$P[\text{ALIVE} @ t | \text{BAD}] = e^{-2\lambda t}$$

I WANT  $P[\text{ALIVE} @ t]$ 

USE TOTAL PROB THM.

$$\begin{aligned} P[\text{ALIVE}] &= P[\text{ALIVE} | \text{GOOD}] P[\text{GOOD}] \\ &\quad + P[\text{ALIVE} | \text{BAD}] P[\text{BAD}] \\ &= e^{-\lambda t} \cdot .9 + e^{-2\lambda t} \cdot .1 \end{aligned}$$

~~$$= P[\text{GOOD} | \text{ALIVE}]$$~~

WANT

~~$$P[\text{GOOD} | \text{ALIVE}] = \frac{P[\text{GOOD} \cap \text{ALIVE}]}{P[\text{ALIVE}]}$$~~

$$= \frac{P[\text{GOOD} \cap \text{ALIVE}]}{P[\text{ALIVE}]}$$

WE WANT

2

$$P[\text{GOOD}|\text{ALIVE}]$$

$$9e^{-t} + 1e^{-2t}$$

KNOW  $P[\text{GOOD}|\text{ALIVE}] \cdot P[\text{ALIVE}] =$   
 $P[\text{GOOD} \cap \text{ALIVE}]$

$$P[\text{GOOD}|\text{ALIVE}] = \underbrace{P[\text{ALIVE}|\text{GOOD}]}_{e^{-t}} \underbrace{P[\text{GOOD}]}_{.9}$$

$$P[A|B] = \frac{P[A \cap B]}{P[B]} \rightarrow P[A|B]P[B] = P[A \cap B]$$

$$P[\text{GOOD}|\text{ALIVE}] = \frac{P[\text{GOOD} \cap \text{ALIVE}]}{P[\text{ALIVE}]} = \frac{.9e^{-t}}{.9e^{-t} + 1e^{-2t}}$$

WE WANT  $t \rightarrow P[G|A] \geq .99$

I WOULD PLOT IT + LOOK.

DO YOU HAVE EBOLA? 4

D: EVENT THAT YOU DO POSIT. }  
D':

WE HAVE AN IMPERFECT TEST.  
T: EVENT THAT YOU TEST POSITIVE-  
Ti -VE.

$P[T|D] = .99$  .01 FALSE-VE.

$P[T|D'] = .05$  FALSE+VE.

$P[D] = 0.001$  PRIOR

RUN THE TEST.

$P[T] = P[T|D]P[D] + P[T|D']P[D']$   
 $= .99 \times .001 + .05 \times .999$   
 $= .00099 + .04995 = .05094$

~~$P[D|T] = \frac{P[D \cap T]}{P[T]}$~~   
 $P[D \cap T] = P[D|T]P[T] = P[D \cap T]$   
 $\frac{.99 \times .001}{.05094} = .00099$

$P[D|T] = \frac{P[D \cap T]}{P[T]} = \frac{.001}{.05} = .02$

$P[D|T] \ll P[D]$  BUT  $\ll$

# NOISY CHANNEL

4

~~P(A)~~ A: TRANSMIT "1"

B: RCV "1"

$P(A) = .01$

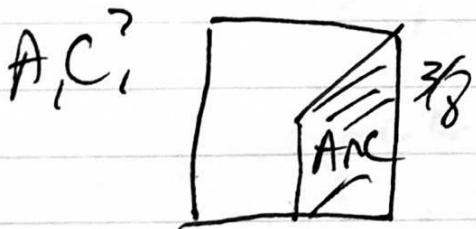
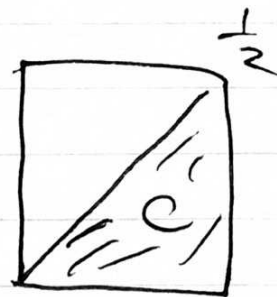
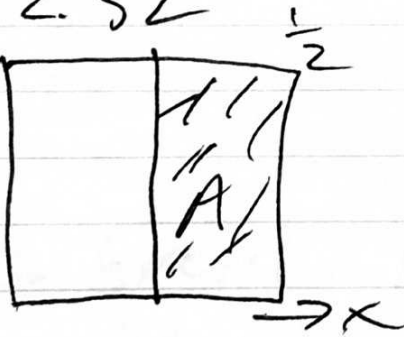
$P(B|A) = .9$

$P(B'|A) = .8$

$P(B) ?$

$P(A|B)$

EX 2.32



A ∩ B ∩ C

$\frac{1}{2} + \frac{1}{2} \neq \frac{3}{8}$

DEP

TOSS OCTAHEDRON

5

$$P[7] = \frac{1}{8}$$

TOSS 4 TIMES.

I WANT  $P[\text{EXACTLY 2 7's}]$

$$P = \frac{1}{8} \quad N = 4 \quad K = 2$$

$$\binom{4}{2} \left(\frac{1}{8}\right)^2 \left(\frac{7}{8}\right)^2 = 6 \cdot \frac{49}{64}$$

$$= \frac{4!}{2!2!}$$

$$\approx .07$$

$$= 6$$

NEW EVENT: NUMBER IS PRIME  
 $P(\text{PRIME}) = \frac{1}{2}$   
2, 3, 5, 7

$P[\text{EXACTLY 2 PRIME OF 4}]$

$$\binom{4}{2} \left(\frac{1}{2}\right)^2 \left(\frac{1}{2}\right)^2 = .375$$

$$P[\text{EXACTLY 3 PRIMES}] = \binom{4}{3} \left(\frac{1}{2}\right)^3 \left(\frac{1}{2}\right) = \frac{4}{16} = .25$$

$$P[\text{OCTAAT SHOWERS}] = \frac{1}{8} \quad \boxed{6}$$

$$P[k \text{ OF } 4] = \binom{4}{k} \left(\frac{1}{8}\right)^k \left(\frac{7}{8}\right)^{4-k}$$

$$P[0 \text{ OF } 4] = \left(\frac{7}{8}\right)^4$$

$$P[1 \text{ OF } 4] = 4 \binom{4}{1} \left(\frac{1}{8}\right) \left(\frac{7}{8}\right)^3 =$$

$$2 \text{ OF } 4 \quad 6 \binom{4}{2} \left(\frac{1}{8}\right)^2 \left(\frac{7}{8}\right)^2$$

$$3 \quad 4 \binom{4}{3} \left(\frac{1}{8}\right)^3 \left(\frac{7}{8}\right)$$

$$4 \quad \left(\frac{1}{8}\right)^4$$

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$$\sum = 1$$

$$\sum_{k=0}^n \binom{n}{k} p^k (1-p)^{n-k} = 1$$

PROOF

$$(p + (1-p))^n = 1 \quad 7$$

$$= \sum_{k=0}^n \binom{n}{k} p^k (1-p)^{n-k}$$

~~Q.E.D.~~