

3/19/18 p

$$f(x) = \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2}}$$

$\mu = 0$ $\sigma = 1$

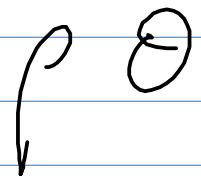
$$A = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} e^{-\frac{x^2}{2}} dx$$

$$A = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} e^{-\frac{1}{2}x^2} dx$$

$$A^2 = \frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} e^{-\frac{x^2+y^2}{2}} dx dy$$

That's integrating over the whole plane. Change variables

$$\begin{aligned} x &= r \cos \theta \\ y &= r \sin \theta \end{aligned}$$



$$x^2 + y^2 = r^2$$

2

$$x = r \cos \theta$$

$$y = r \sin \theta$$

$$\frac{dx}{dr} = \cos \theta$$

$$\frac{dx}{d\theta} = -r \sin \theta$$

$$\frac{dy}{dr} = \sin \theta$$

$$\frac{dy}{d\theta} = r \cos \theta$$

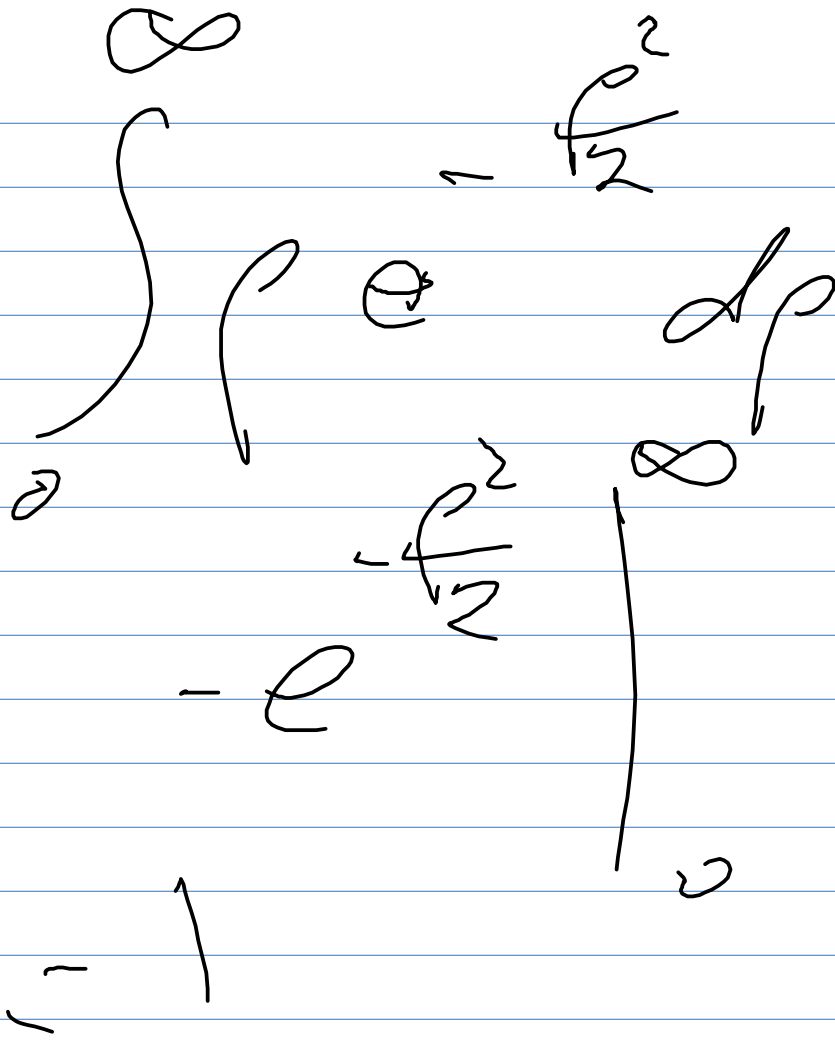
$$J = \begin{vmatrix} \cos \theta & -r \sin \theta \\ \sin \theta & r \cos \theta \end{vmatrix}$$

$$= r$$

$$dx dy = r dr d\theta$$

$$\int_0^{2\pi} \int_0^R r dr d\theta = \int_0^{2\pi} \left[\frac{r^2}{2} \right]_0^R d\theta = \int_0^{2\pi} \frac{R^2}{2} d\theta = \frac{R^2}{2} \int_0^{2\pi} 1 d\theta = \frac{R^2}{2} \cdot 2\pi = \pi R^2$$

$$\int_0^{2\pi} \int_0^R r dr d\theta = \pi R^2$$

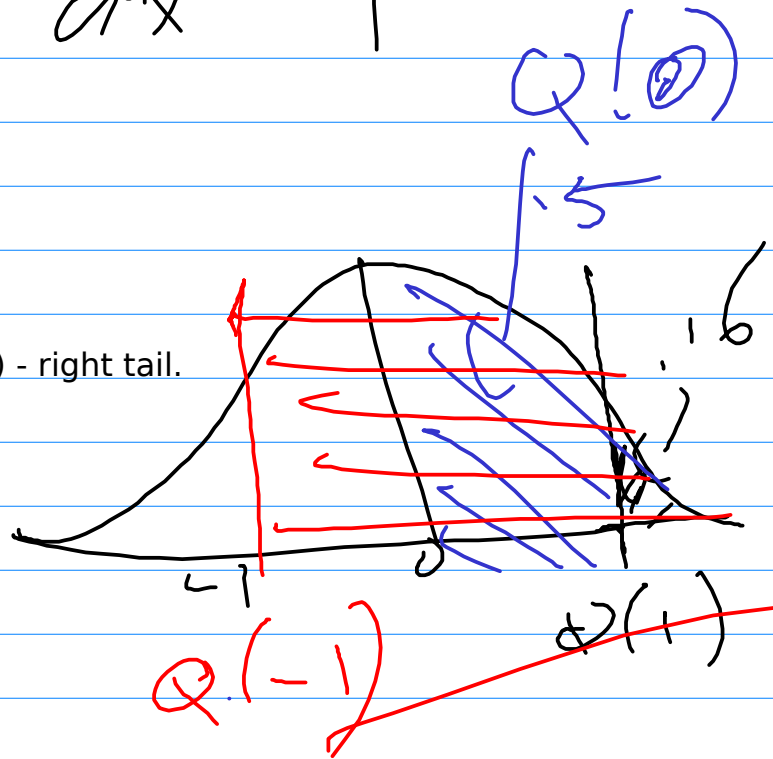


exponent: rho squared over two, minus

3

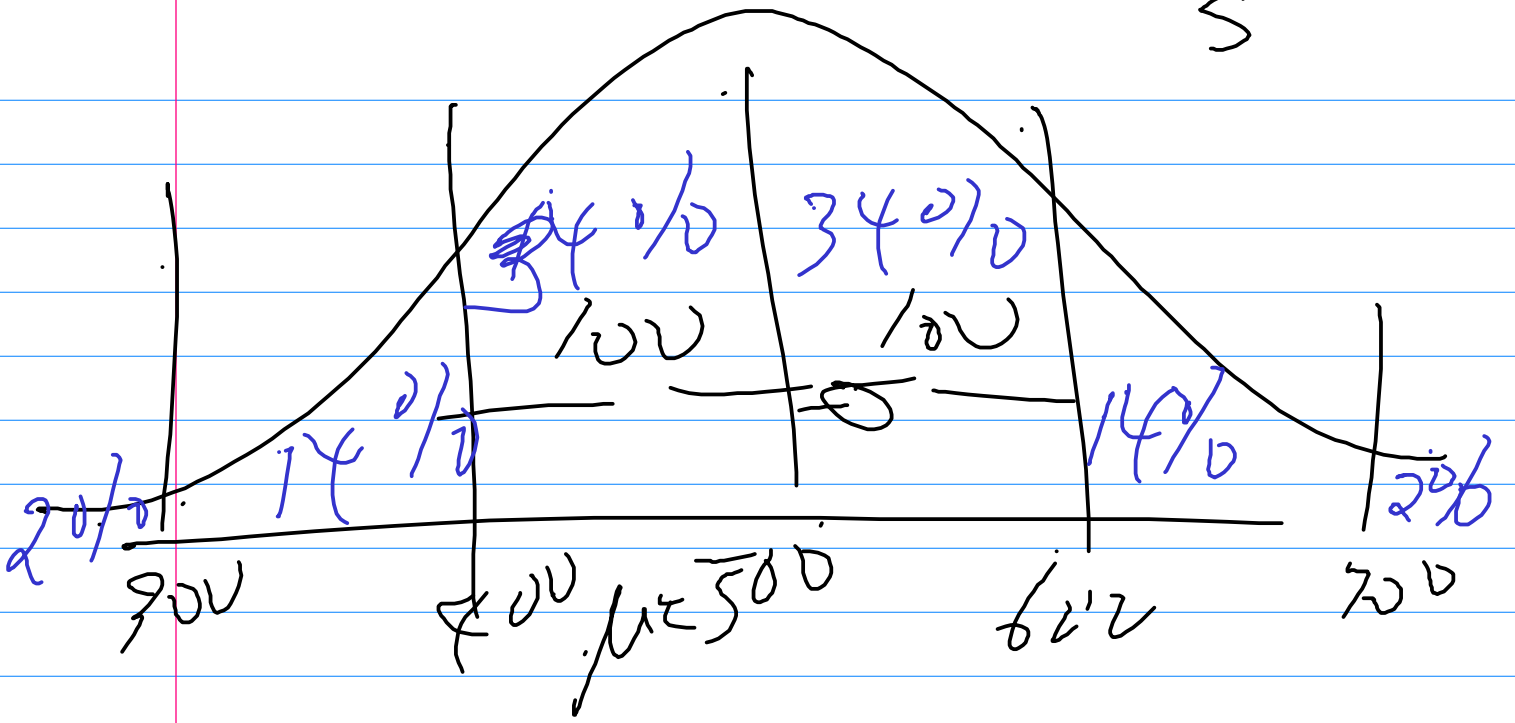
$$\int_{-\infty}^{\infty} \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2}} dx = 1$$

book page 168 has table of $Q(x)$ - right tail.



how to find $q(-1)$? It's not in table. Integral from $-\infty$ to -1 = int from 1 to ∞ .
 $= .16$. Int from -1 to ∞ is $1 - (\text{int from } -\infty \text{ to } -1) = 1 - .16 = .84$.
 That table has $m=0, s=1$.

5



homework: book 4.85 on p 223.

I'll do a special case. x is $N(0,10)$. y is $N(100,100)$.

$y=ax+b$. What are a,b ?
sigma scales by a , so $a=10$.
mean transforms to mean
 $100=10x+b$ $b=100$.
 $y=10x+100$

example 2 transform SAT $N(500,100)$ to standard $N(0,1)$.

$y=.01 x - 5$.

500 \rightarrow 0. 600 \rightarrow 1. 200 \rightarrow -3.

$N(m,s)$ means normal dist with mean m and std s .

4.90

 $\text{var}=2 \rightarrow s=1.4$ do this for $R=1$.

$$y=x^2.$$

$$dy/dx = 2x$$

$$F(x) = \text{prob}(X \leq x).$$

$$F(y) = \text{prob}(Y \leq y) = \text{prob}(Y \leq x^2)$$

Example 5.5 p 253

