

4 STUDENTS

A B C D

DIVIDE INTO 2

TEAMS OF 2.

UNDEFINED: DO 2 TEAMS
HAVE NAMES?

AB, CD

AC, BD

AD, BC

BC AD

BD, AC

CD, AB

6

4 CHOICES
FOR 1ST
PLAYER.

3 FOR 2nd

PICKS EACH
TEAM TWICE.

Q: does the order of the players in each team matter?

Is the 1st player the captain?

If doesn't matter: 6 possibilities.

If it does: $4 \times 3 \times 2 = 24$

2

2c

how many 5-card hands?

1st card: 52

2nd: 51

...

5 cards: $52 \times 51 \times 50 \times 49 \times 48 = 52!/47!$

but this ignored that I don't care about the order

how many ways could I have picked each hand? 5! ways

hands: $52!/47!/5!$

easy example: 6 card deck. pick a hand of 3 cards.

card names: a b c d e f

6 choices for 1st card

then 5 choices for 2nd

then 4 for the 3rd card. gives $6 \times 5 \times 4 = 6!/3! = 120$

$6! = 6 \times 5 \times 4 \times 3 \times 2 \times 1$

$3! = 3 \times 2 \times 1$

$6!/3! = 6 \times 5 \times 4$

But the above called these 2 hands different: abc and bca.
If I don't care about the order I picked the cards in my hand,
then I have to divide by the number of ways I could have
picked each hand. That's 6.

These hands are the same: abc acb bac bca cab cba 6

That's $120/6 = 20$ hands.

abc abd abe abf acd ace acf ade adf aef

bcd bce bcf bde bdf bef

cde cdf cef

def

That's 20.

If the order does matter. To pick k cards from a deck of n .
 # hands is $n(n-1)(n-2)\dots(n-k+1) = n!/(n-k)!$

This assumes that the cards are all different.

If order does not matter, divide that by $k!$
 Answer is $n!/(n-k)!/k! = n \text{ choose } k =$

$$\binom{n}{k}$$

2e

How many ways to pick 5 widgets?

$$\binom{100}{5}$$

How many ways to pick 5 good widgets?

$$\binom{90}{5}$$

Probability of all 5 widgets good:

$$\frac{\binom{90}{5}}{\binom{100}{5}}$$

$$\frac{90!}{85! 5!} \cdot \frac{95! 5!}{100!} =$$

9/

C/c

sample w replacement order matters
 urn has 3 colors: r g b
 pick 5 balls w replacement.
 rrrrr ggggg rrrrg rrgrr rgrbr

3 colors for 1st x 3 colors for 2nd x 3 colors for 3rd...
 $3 \times 3 \times 3 \times 3 \times 3 = 3^5 = 243$.

Permutations: select k from n. Order matters: $n!/(n-k)!$

18 Pick 4 teams of 10 players from 40 players. How many teams?

pick 1st team: $40 \times 39 \times 38 \dots \times 31 / 10! = 40! / 30! / 10!$
 2nd team: $30 \times 29 \dots \times 21 / 10! = 30! / 20! / 10!$
 3rd team: $20! / 10! / 10!$
 4th team: 1

result: $40! 30! 20! / (30! 20! 10! 10! 10! 10!)$ agrees
 order within each team does not matter
 here, order between teams does.
 sometimes it does not.



